

Standard Model

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44. Herbstschule für Hochenergiephysik, Maria Laach
04. - 14. September 2012

- Lecture 1: Formulation of the Standard Model
- Lecture 2: Precision tests of the Standard Model
- Lecture 3: NLO Calculations for the LHC
- Lecture 4: Higgs physics at the LHC

NLO calculations for the LHC

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- Physics at the LHC
- Relevance of NLO (QCD) corrections
- Calculation of NLO corrections
- Relevance of Electroweak Radiative Corrections
- Example processes

Physics at the LHC

Some important SM measurements and relevant processes:

- improved measurement of W -boson mass M_W
main process: $pp \rightarrow W \rightarrow l\nu_l + X$
- improved measurement of effective weak mixing angle $\sin^2 \theta_{\text{eff}}$
main process: $pp \rightarrow Z \rightarrow ll + X$
- improved measurement of non-Abelian gauge couplings
main processes:
 - ▶ $pp \rightarrow W\gamma, Z\gamma + X$
 - ▶ $pp \rightarrow WW, WZ, ZZ + X$
- improved measurement of top-quark mass
main process $pp \rightarrow tt + X$
- search for the Higgs boson and measurement of its properties
different production and decay processes

New physics may reveal itself by

- spectacular new signatures that are easily distinguishable from the Standard Model
example: new resonance in $\mu^+\mu^-$ like a Z'
so far nothing of this sort found
- less spectacular signatures with Standard Model background
(e.g. excess)
example: missing energy in production of supersymmetric particles
⇒ need SM prediction
- (small) deviations from Standard Model predictions
examples: anomalous couplings,
contributions of heavy degrees of freedom via loop processes
⇒ need precise SM prediction

In the absence of striking new signatures,
to distinguish new physics from SM effects
precise predictions of SM processes are necessary!

Relevance of NLO (QCD) corrections

QCD corrections: substantial part of predictions

- **LO predictions** depend on $\alpha_s = \alpha_s(\mu)$, scale μ free parameter
 \Rightarrow large scale uncertainty (up to factor 2)
 \Rightarrow often no quantitative prediction possible
 μ dependence due to missing higher orders

- **NLO predictions:** reduced scale uncertainty
first real prediction

\Rightarrow needed for all scattering processes at the LHC

$$\mathcal{O}(\alpha_s) \times \log(\dots) \sim 10\% - 100\%, \quad \alpha_s(M_Z) \approx 0.12$$

- **NNLO predictions:** scale uncertainty further reduced
first real uncertainty estimate

\Rightarrow needed for light-candle processes like

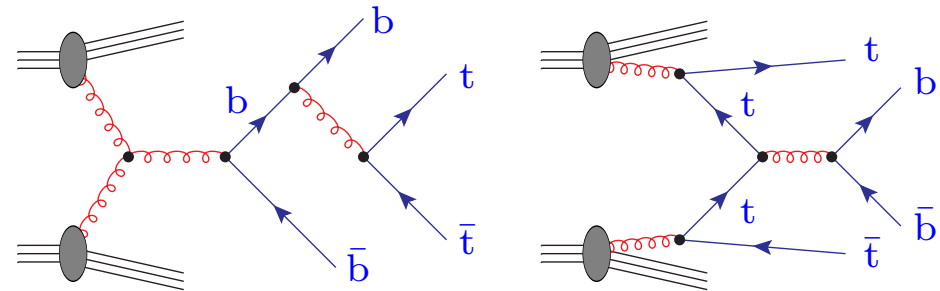
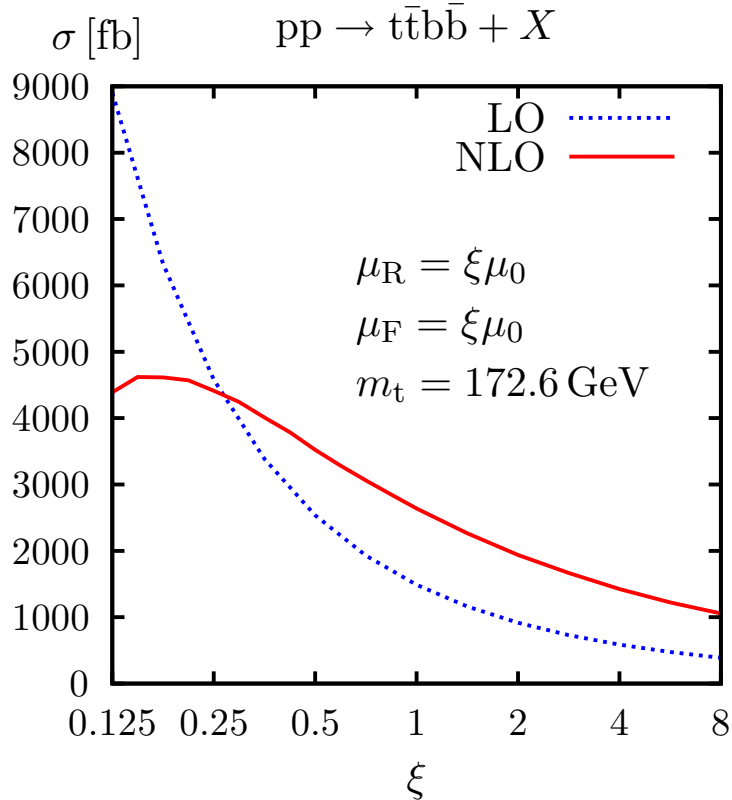
single W/Z production, $t\bar{t}$ production

$$\mathcal{O}(\alpha_s^2) \times \log^2(\dots) \sim \text{few}\% - 20\%$$

\hookrightarrow **NLO (NNLO) corrections important for reliable predictions**

Background process to
 $pp \rightarrow t\bar{t}H + X \rightarrow t\bar{t}b\bar{b} + X$

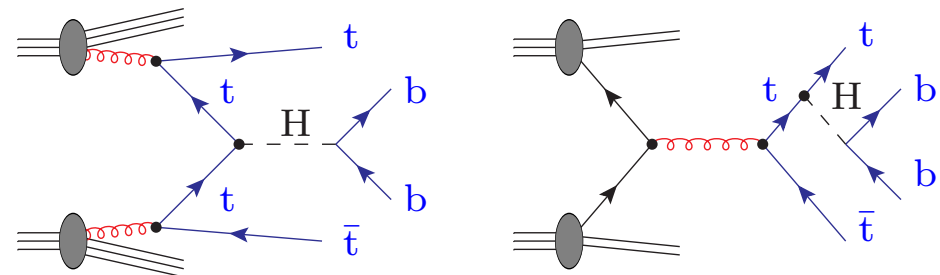
Bredenstein, Denner, Dittmaier, Pozzorini '10



$LO \propto \alpha_S(\mu_R)^4 \Rightarrow$ large scale uncertainty

μ_F	$m_t/8$	$m_t/4$	$m_t/2$	m_t	$2m_t$	$4m_t$	$8m_t$
$\alpha(\mu_F)$	0.151	0.133	0.119	0.108	0.098	0.091	0.084
$\frac{\alpha(\mu_F)}{\alpha(m_t)}$	1.40	1.24	1.11	1.00	0.91	0.84	0.78
$\left(\frac{\alpha(\mu_F)}{\alpha(m_t)}\right)^4$	3.88	2.34	1.49	1.00	0.70	0.50	0.37

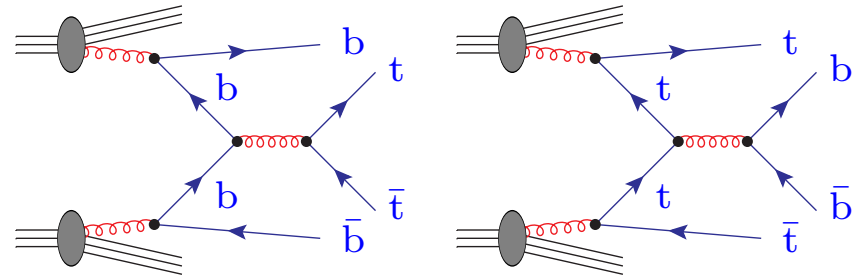
original (ATLAS) scale choice based on $t\bar{t}H$



$$\mu_0 = E_{\text{thr}}/2 = m_t + m_{b\bar{b}}/2$$

\Rightarrow large K factor (1.8) and scale dependence (34%)

QCD dynamics of $t\bar{t}H$ and $t\bar{t}b\bar{b}$ different



various different channels for $t\bar{t}b\bar{b}$

good central scale

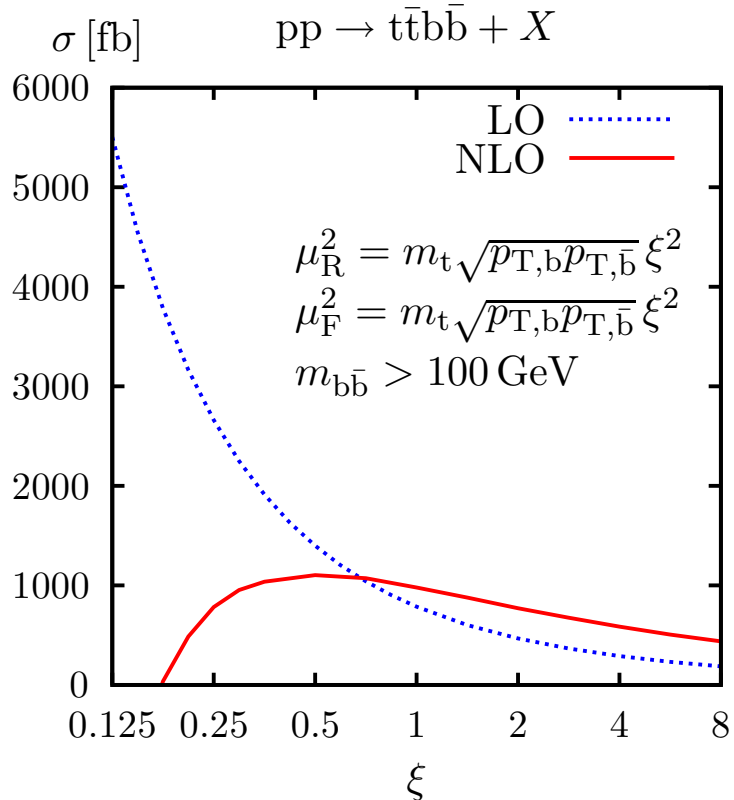
$$\mu_0^2 = m_t \sqrt{p_{T,b} p_{T,\bar{b}}}$$

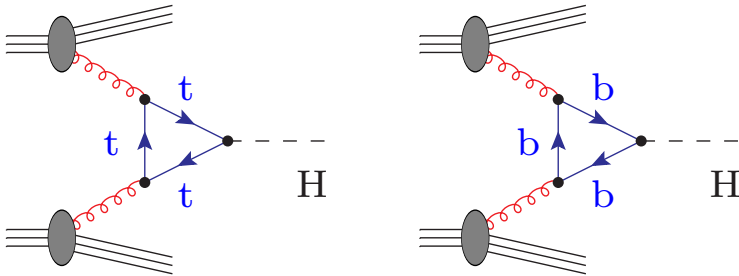
one α_s at scale m_t

one α_s at scale of p_T of b quarks

- small correction and uncertainty:
 $K = 1.24 \pm 21\%$
- central scale close to a maximum

Bredenstein, Denner, Dittmaier, Pozzorini '10





- most important production channel at LHC

- $\sigma_{LO} \propto \alpha_s^2$

strong dependence on factorization and renormalization scales (100%)
 \Rightarrow higher-order corrections very important

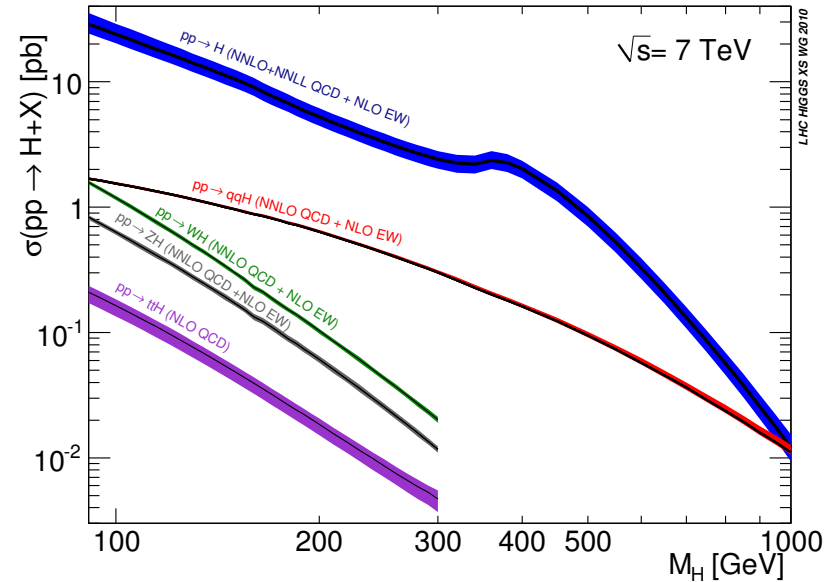
- complete NLO: 80–100%

virtual contribution $\pi\alpha_s \sim 35\%$ [$\pi^2(\alpha_s/\pi)$]

real contribution $\sim 50\%$

- NNLO: $\sim 25\%$

LHC HIGGS XS WG '11



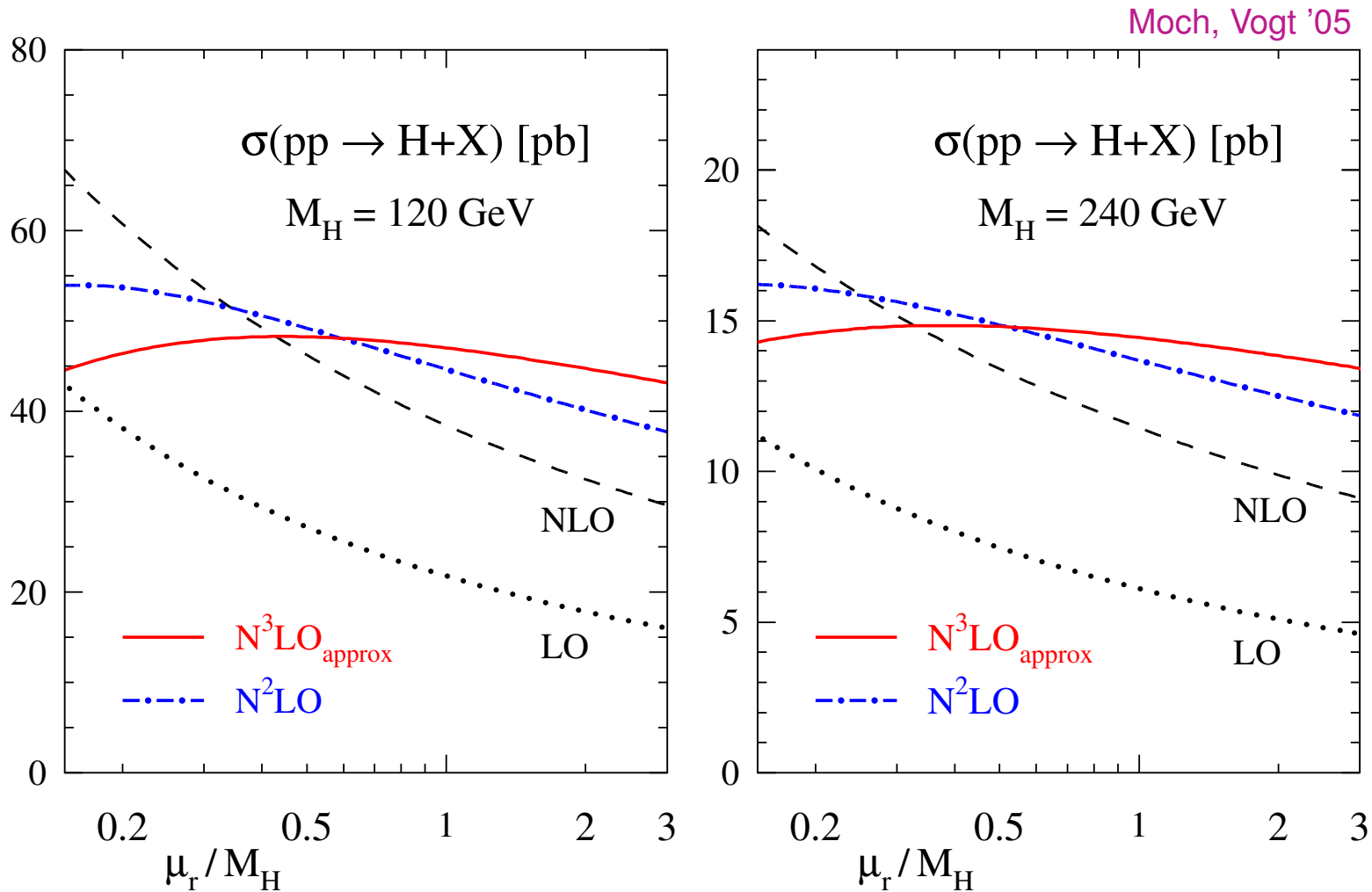
Graudenz, Spira, Zerwas '93

Djouadi, Graudenz, Spira, Zerwas '95

Harlander, Kilgore '01, '02; Catani, de Florian, Grazzini '01

Anastasiou, Melnikov '02; Ravindran, Smith, van Neerven '03, '04

Ahrens, Becher, Neubert, Yang '08

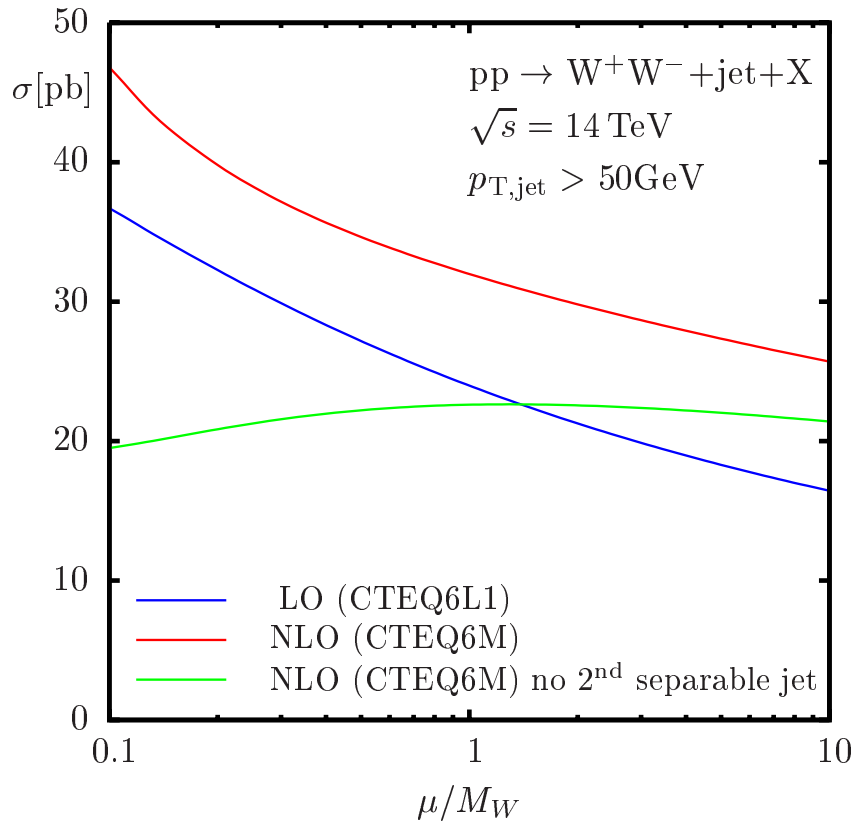


Reduction of renormalization scale dependence with increasing orders!

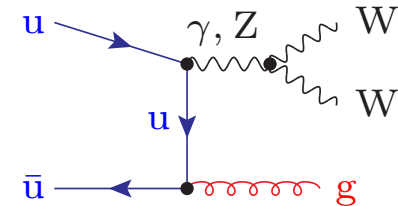
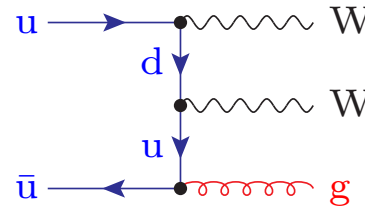
\Rightarrow residual scale uncertainty $\lesssim 5\text{--}10\%$

Appearance of new channels:

Dittmaier, Kallweit, Uwer '07



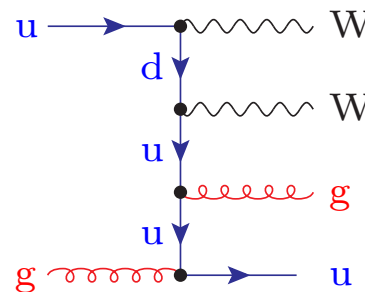
• $\sigma_{\text{LO}} \propto \alpha_s$



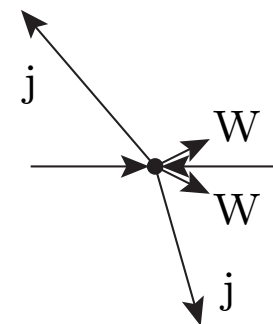
• scale dependence stabilises at NLO for genuine $WW + j$ production

• significant scale dependence is introduced by $WW + 2j$ (difference between green and red curves)

new diagrams



new configuration



Most signal processes involve few final-state particles:

- $2 \rightarrow 2$ $pp \rightarrow ll, W\gamma, WW, tt, \dots + X$
- $2 \rightarrow 3$ $pp \rightarrow Hjj, WW\gamma, \dots + X$

However,

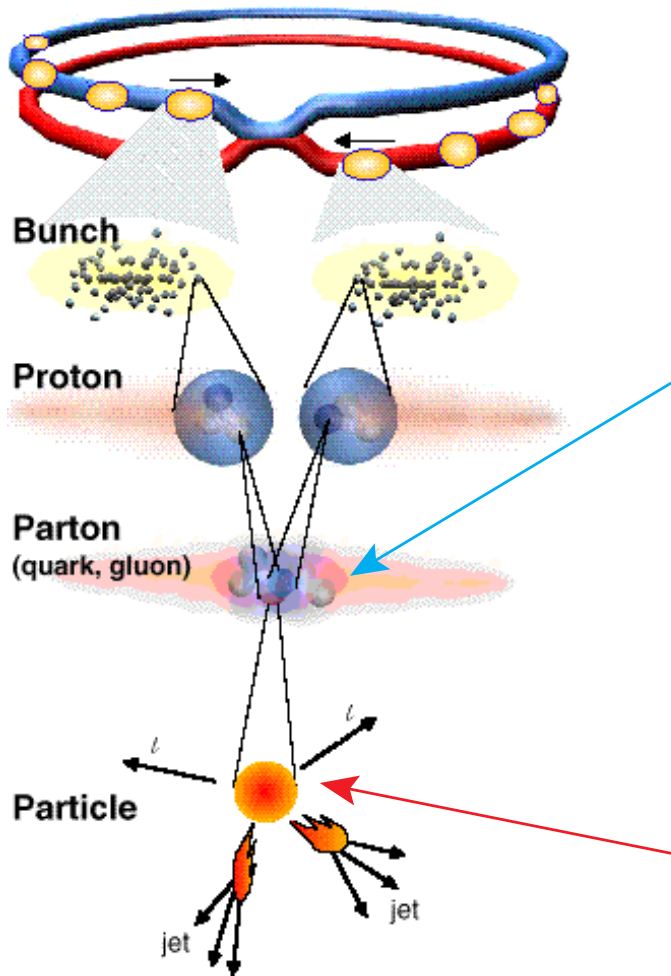
- **heavy particles** (W, Z, t, \dots) **decay** into jets, leptons, photons
 $pp \rightarrow WW \rightarrow ll\nu_l\nu_l + X, pp \rightarrow tt \rightarrow b\nu_e\bar{b}\mu\nu_\mu + X$
- **irreducible backgrounds** involve genuine multiparticle final states
 $pp \rightarrow ll\nu_l\nu_l + X, pp \rightarrow b\nu_e\bar{b}\mu\nu_\mu + X$
 (backgrounds often not fully accessible to measurements)
- large fraction of final states contains **additional jets**
 $pp \rightarrow WWj + X, pp \rightarrow WWjj + X, \dots$

\Rightarrow **Need reliable predictions for multiparticle processes!**

NLO calculations

- $2 \rightarrow 2$ **trivial** (textbook)
- $2 \rightarrow 3$ **standard** (many groups)
- $2 \rightarrow 4$ **state of the art** (several groups)
 - $pp \rightarrow t\bar{t}b\bar{b}$ Bredenstein, Denner, Dittmaier, Pozzorini '09, Bevilacqua et al. '09
 - $pp \rightarrow t\bar{t}jj$ Bevilacqua, Czakon, Papadopoulos, Worek '10
 - $pp \rightarrow W^+W^-b\bar{b}$ Denner, Dittmaier, Kallweit, Pozzorini '10; Bevilacqua et al. '10
 - $pp \rightarrow W^+W^\pm jj$ Melia, Melnikov, Rontsch, Zanderighi '10, '11; Greiner et al. '12
 - $pp \rightarrow Wjjj$ Berger et al. '09; R.K.Ellis et al. '09
 - $pp \rightarrow Zjjj$ Berger et al. '10
 - $pp \rightarrow b\bar{b}b\bar{b}$ Binoth et al. '09
 - $pp \rightarrow jjjj$ Bern et al. '11
- $2 \rightarrow 5$ **only very few** (one group)
 - $pp \rightarrow Wjjjj$ Berger et al. '10
 - $pp \rightarrow Zjjjj$ Berger et al. '11

Calculation of NLO corrections



parton content of the proton:
 valence quarks uud ,
 sea quarks $u, d, c, s, (+b,) +$ antiquarks
 gluons g (+ photons γ)

“parton distribution functions” (PDFs) $f_{i/p}(x, \mu_F)$
 probability for parton i to have fraction x
 of momentum p at “factorization scale” μ_F
 = non-perturbative input (from experiment)
 process independent

hard interaction of partons
 \hookrightarrow perturbative QFT applicable,
 model for hard interaction
 (except QCD/QED) only enters here

$$\sigma_{pp \rightarrow F+X}(p_1, p_2) = \int_0^1 dx_a \int_0^1 dx_b \sum_{a,b} f_{a/p}(x_a, \mu) f_{b/p}(x_b, \mu_F) \hat{\sigma}_{ab \rightarrow F}(x_a p_1, x_b p_2, \mu_F)$$

LO partonic cross section for a $2 \rightarrow n$ process can be written as

$$d\sigma_{\text{LO}} = \frac{1}{2s} \int d\Phi_n |\mathcal{M}_{\text{LO}}|^2$$

$$\int d\Phi_n = (2\pi)^4 \delta^{(4)} \left(P - \sum_{i=1}^n q_i \right) \prod_{i=1}^n \frac{d^3 q_i}{(2\pi)^3 2E_i} \quad n\text{-particle phase space}$$

\mathcal{M}_{LO} : LO matrix element (contains model for hard interaction)

$s = P^2 = (\hat{p}_1 + \hat{p}_2)^2$ square of centre-of-mass energy of hard process ($\hat{p}_i = x_i p_i$)

Integration over phase space by Monte Carlo methods \Rightarrow

- any distribution can be determined simultaneously
- Monte Carlo events can be unweighted

Many codes exist at LO:

- MADGRAPH Alwall, Herquet, Maltoni, Mattelaer, Stelzer
- WHIZARD Kilian, Ohl, Reuter
- SHEPRA Höche, Krauss, Schuhmann, Siegert, Winter
- HELAC Papadopoulos, Worek
- ... many more

- **Feynman diagrams:** double factorial complexity $[2n!! = 2n(2n - 2)(2n - 4)...2]$

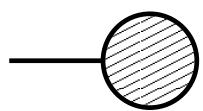
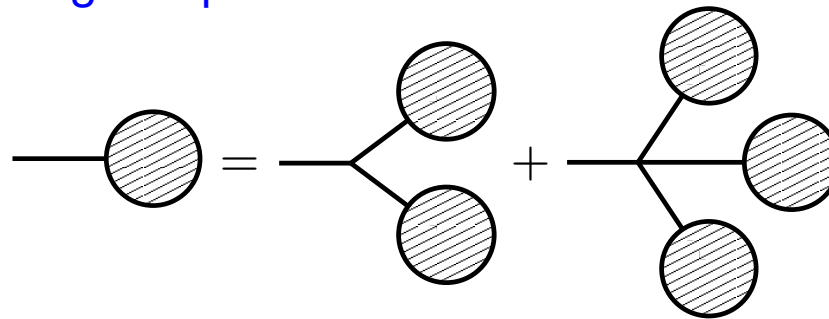
diagrams for pure gluon (scalar) processes

external gluons	4	5	6	7	8	9	...	n
# diags w/ only 3-g vertices	3	15	105	945	10395	135135		$(2n - 5)!!$
# diags w/ 3-g and 4-g vert.	4	25	220	2485	34300	559405		

- **recursion-relation technique:** polynomial complexity of rank 4: $\mathcal{O}(n^4)$

Berends, Giele '88; Kleiss, Kuijf '89, Caravaglios, Moretti '95, Draggiotis, Kleiss, Papadopoulos '98

based on **Dyson–Schwinger equations**



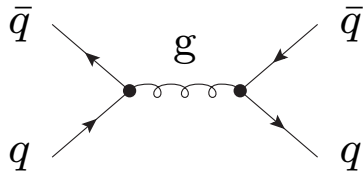
: **off-shell current** with arbitrary number of on-shell lines

: sub-amplitude with one off-shell and arbitrary many on-shell lines

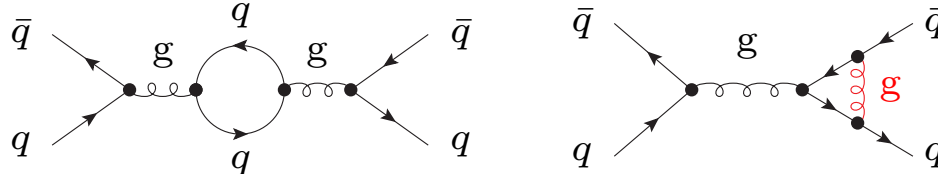
starting point of iteration: = wave function (polarization vector)

NLO corrections consist of Feynman diagrams of higher order to the same process:

tree diagrams



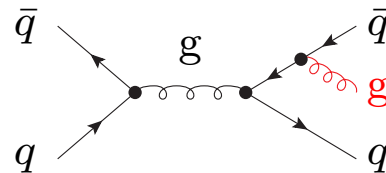
loop diagrams



loop diagrams contain infrared singularities
from internal gluons soft or collinear to quarks

Process with an additional gluon has to be added to cancel IR singularities

(soft or collinear photons cannot be separated experimentally!)



Square of bremsstrahlung matrix element of the same order as interference between LO diagrams and loop diagrams!

Some collinear singularities from the initial state do not cancel but can be absorbed by a renormalization of the PDFs \Rightarrow collinear counter term

NLO partonic cross section can be written as

NLO partonic cross section can be written as **in subtraction method**

$$d\sigma_{\text{NLO}} = \int d\Phi_n \left[|\mathcal{M}_{\text{LO}}|^2 + 2 \operatorname{Re}\{\mathcal{M}_{\text{LO}}^* \mathcal{M}_{\text{NLO,V}}\} + C + \int d\Phi_1 \sum_j S_j \right] \\ + \int d\Phi_{n+1} \left[|\mathcal{M}_{\text{NLO,R}}|^2 - \sum_j S_j \right]$$

$\int d\Phi_{n(+1)}$: n or $n + 1$ particle phase space

$\mathcal{M}_{\text{LO}}, \mathcal{M}_{\text{NLO,V}}, \mathcal{M}_{\text{NLO,R}}$: matrix elements for LO, virtual and real NLO

C collinear counter term from renormalization of PDFs

$\sum S_j$: subtraction terms for real corrections

$\int d\Phi_1 \sum S_j$: (analytically) integrated subtraction terms

subtraction terms cancel but render individual integrals finite \Rightarrow stable numerical integration

$\mathcal{M}_{\text{NLO,R}}$: tree-level matrix elements

subtraction terms S_j : colour-weighted tree-level matrix elements

virtual corrections $\operatorname{Re}\{\mathcal{M}_{\text{LO}}^* \mathcal{M}_{\text{NLO,V}}\}$ (loop diagrams): **require new methods**

Until ~ 2005 : Virtual corrections were the bottleneck of NLO calculations.

- **Feynman diagrams**: worse than factorial complexity
- relied on **process-specific** algebraic calculations, **no full automation**

NLO revolution: *Ossola, Papadopoulos, Pittau '07, Bern, Dixon, Kosower, Britto, Cachazo, Feng, Ellis, Giele, Melnikov, ...*

- **unitarity-cut technique**: polynomial complexity of rank 9: $\mathcal{O}(n^9)$
Giele, Zanderighi '08
- automation immediately performed by different groups

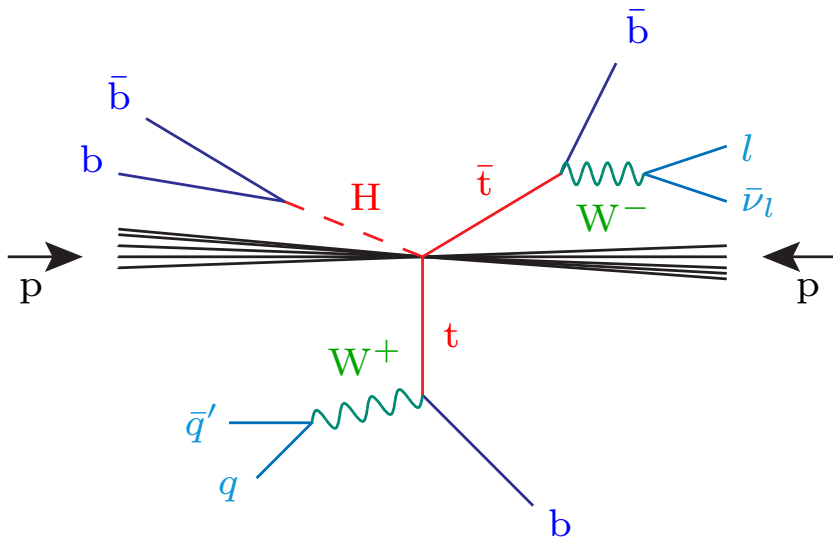
recursion relation technique for NLO:

- exponential complexity: $\mathcal{O}(n^4 2^n)$ *van Hameren '09* (pure gluon amplitudes)

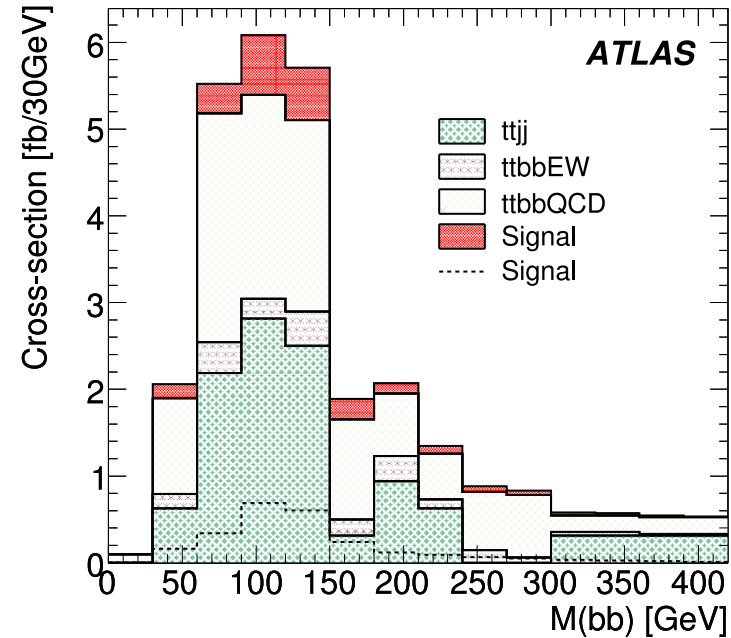
revival of Feynman diagrams:

- Feynman diagrams yield faster codes for $2 \rightarrow 4$ processes
- allow efficient summation over colours and helicities
- asymptotic behaviour not necessarily relevant for practical purposes
- full automation in progress *Cascioli, Maierhofer, Pozzorini '12* OPENLOOPS

Background to $pp \rightarrow t\bar{t}H(\rightarrow b\bar{b})$



“CSC book”, CERN-OPEN-2008-020



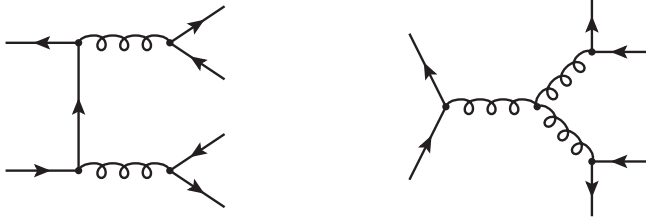
- **relevance:** direct experimental access to $t\bar{t}H$ -Yukawa-coupling
- **problem:** control of background via $pp \rightarrow t\bar{t}b\bar{b}$, $t\bar{t} + \text{jets}$
 need: ▶ improved analysis methods (fat jets, boosted Higgs)
 ▶ NLO predictions for background processes

First complete NLO calculation for a $2 \rightarrow 4$ hadron-collider process

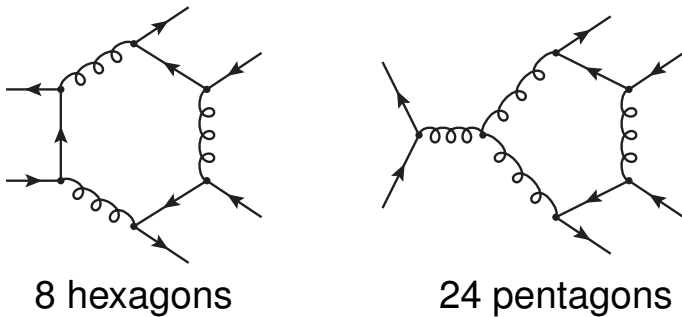
$q\bar{q} \rightarrow t\bar{t}b\bar{b}$ 5% of cross section

Bredenstein, Denner, Dittmaier, Pozzorini '08

LO: 7 diagrams



NLO: 188 diagrams

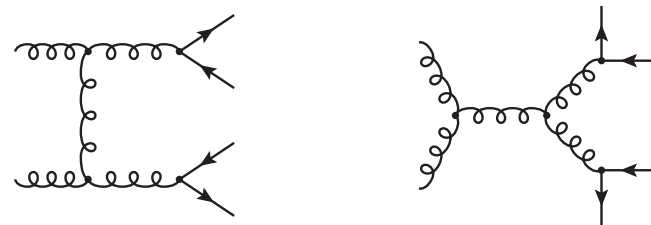


bremsstrahlung diagrams: 64

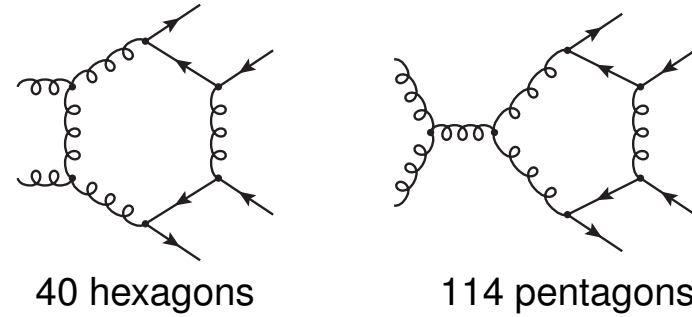
$gg \rightarrow t\bar{t}b\bar{b}$ 95% of cross section

Bredenstein, Denner, Dittmaier, Pozzorini '09

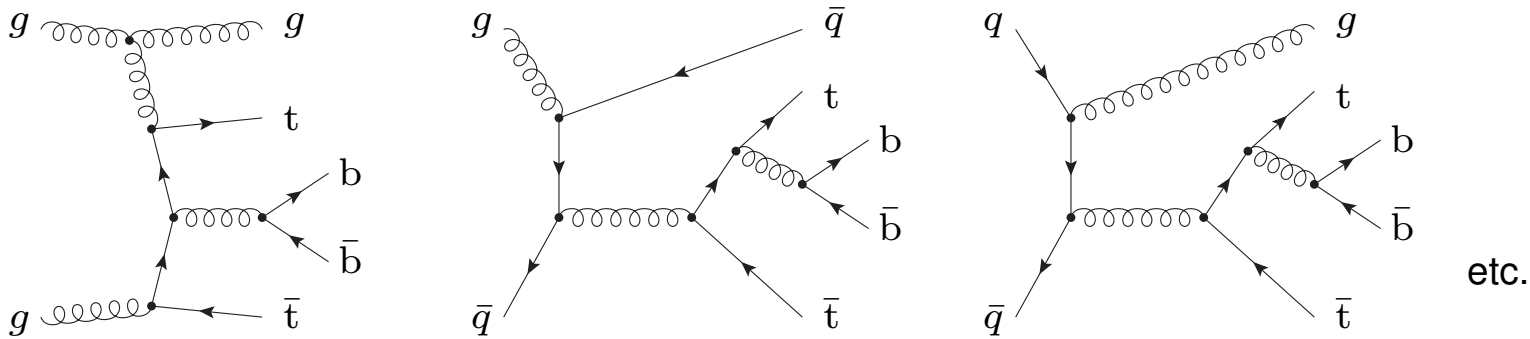
LO: 36 diagrams



NLO: 1003 diagrams

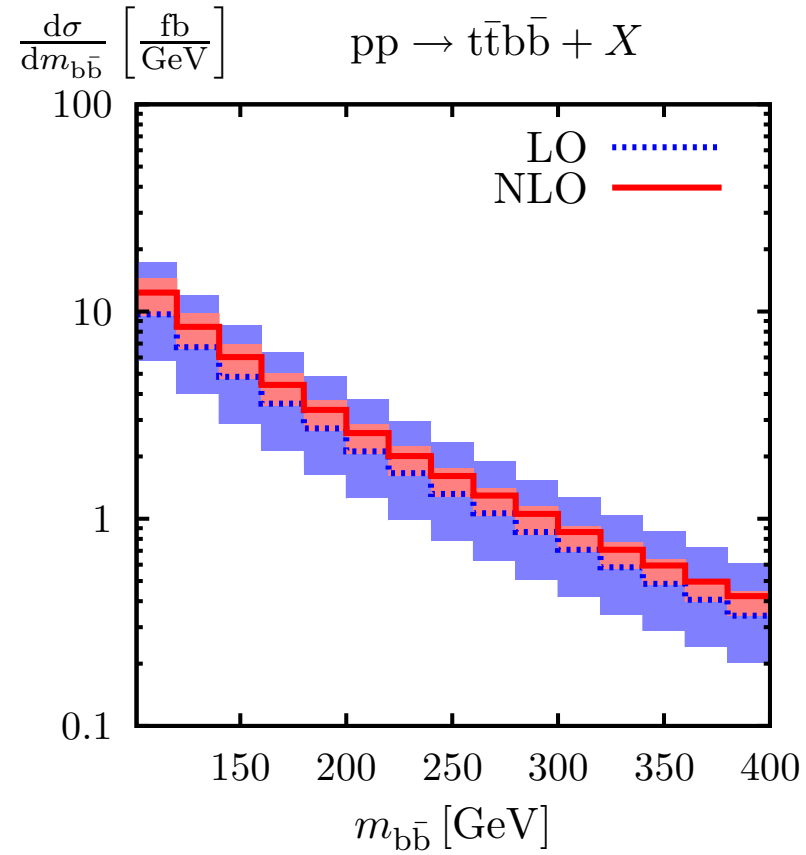
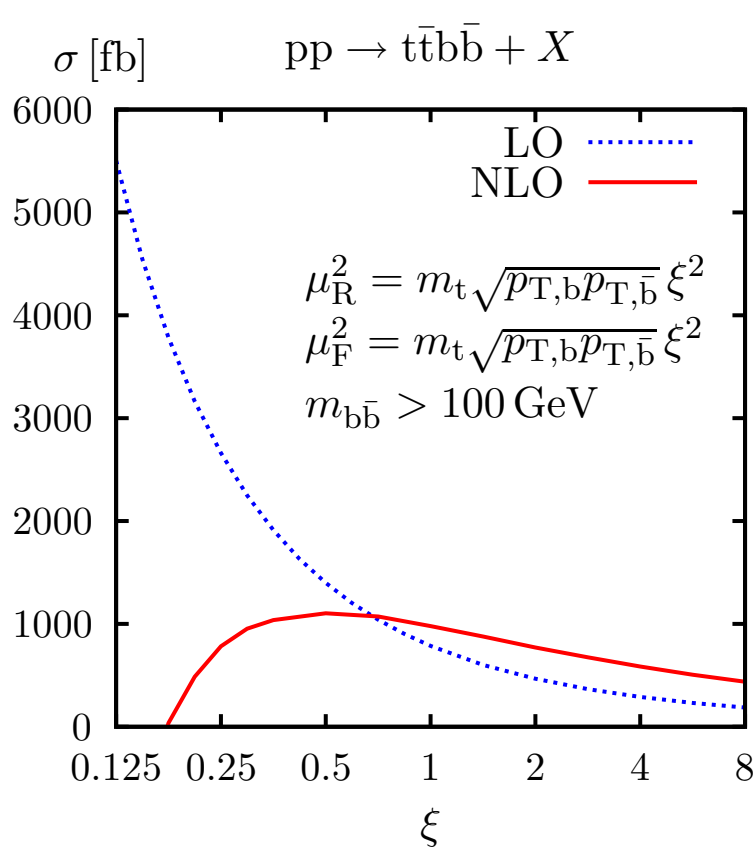


bremsstrahlung diagrams: 341



- **channels:** $gg \rightarrow b\bar{b}t\bar{t}g$, $qg \rightarrow b\bar{b}t\bar{t}q$, $qq \rightarrow b\bar{b}t\bar{t}g$
- numerical (Monte-Carlo-)integration over 11-dimensional phase space
- fast calculation of amplitudes (bremsstrahlung and LO) needed
- treatment of soft and collinear singularities via subtraction method
 \Rightarrow 30 dipole subtraction terms per channel
 \Rightarrow LO matrix element has to be calculated 30 times for each event
- run times: ~ 50 h on single CPU for 10^7 events
 \Rightarrow 0.5% accuracy for total integrated cross section

Bredenstein, Denner, Dittmaier, Pozzorini '09

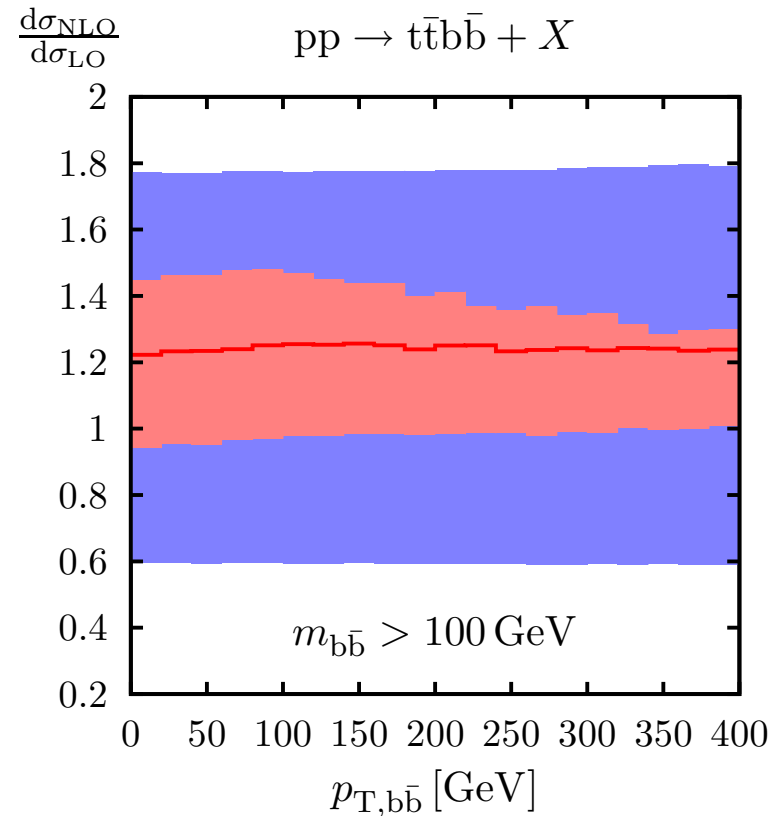
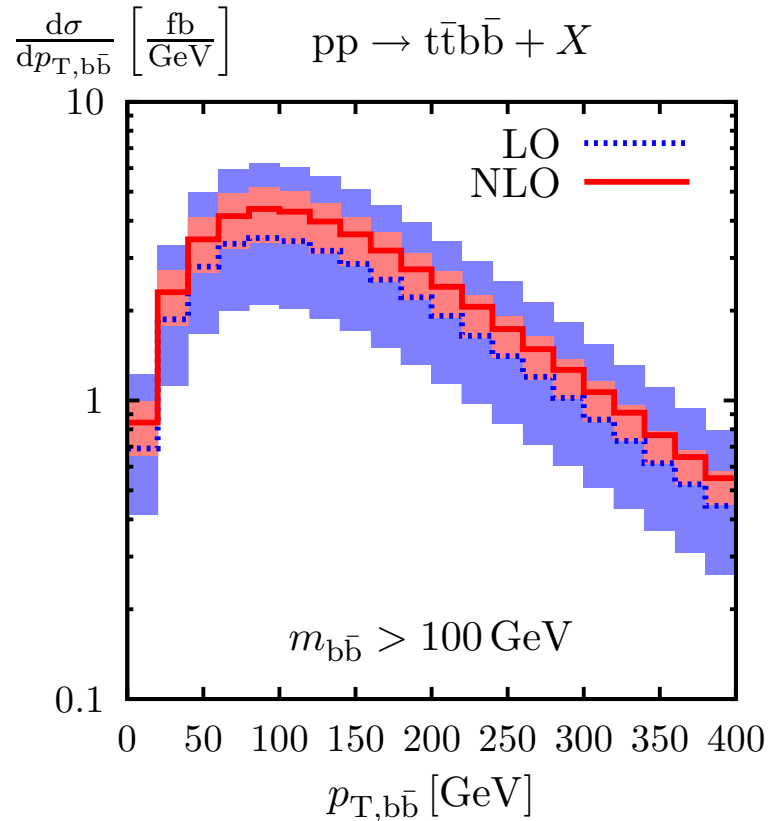


- small NLO correction $K \simeq 1.24$
- reduction of scale uncertainty

$$\Delta_{\text{LO}} \sim 100\% \quad \rightarrow \quad \Delta_{\text{NLO}} \sim 20\text{--}30\%$$

Distribution in transverse momentum of $b\bar{b}$ pair

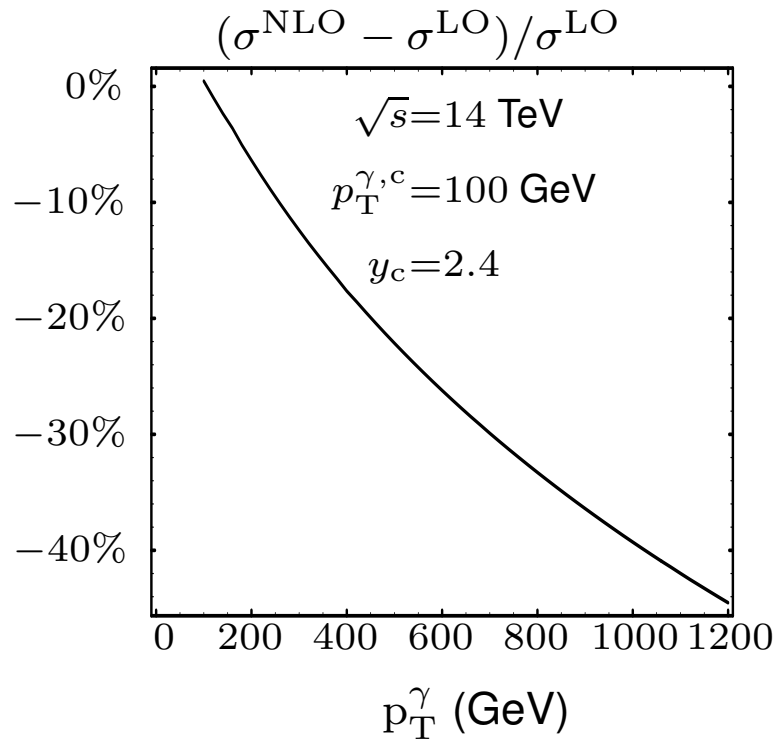
Bredenstein, Denner, Dittmaier, Pozzorini '09



- K -factor almost constant over wide $p_{T,b\bar{b}}$ range for dynamical scale
- NLO-analysis enables suitable dynamic scale choice
 \Rightarrow improvement of LO prediction via rescaling

Relevance of EWRC

- generically: $\mathcal{O}(\alpha) \sim \mathcal{O}(\alpha_s^2) \sim \text{few } \%$
- EW corrections can be enhanced by high energy scales or kinematic effects
example: electroweak corrections to $pp \rightarrow Z\gamma + X$ Hollik, Meier '04



small p_{T}^{γ}

- ▶ corrections of $\mathcal{O}(\alpha) \sim 1\%$

$p_{\text{T}}^{\gamma} \gg 100 \text{ GeV}$

- ▶ large negative corrections $\gg 1\%$
- ▶ increase with p_{T}^{γ}
- ▶ -40% at $p_{\text{T}}^{\gamma} \sim 1 \text{ TeV}$!

- leading NNLO EW corrections might be relevant for some processes
(Drell-Yan, Z+jet, W+jet) $(40\%)^2 = 16\%$

Scattering energy \gg characteristic scale of EW corrections:

$$E_{\text{CMS}} \gg M_{\text{W}} \approx 80 \text{ GeV}$$

\Rightarrow large double logarithms

$$\ln^2 \left(\frac{E_{\text{CMS}}^2}{M_{\text{W}}^2} \right) \sim 25 \quad \text{at} \quad E_{\text{CMS}} \sim 1 \text{ TeV}$$

typical size of corrections:

$$\frac{\alpha}{4\pi s_{\text{W}}^2} \ln^2 \left(\frac{E_{\text{CMS}}^2}{M_{\text{W}}^2} \right) \sim 25\% \quad \text{at} \quad E_{\text{CMS}} \sim 1 \text{ TeV}$$

general feature of hard scattering processes!

Large EW logarithms can be related to mass singularities:

$$M_{\text{W}}/E_{\text{CMS}} \ll 1 \quad \Rightarrow \quad E_{\text{CMS}} \rightarrow \infty \quad \text{or} \quad M_{\text{W}} \rightarrow 0$$

EW logarithms can be calculated with process-independent methods.

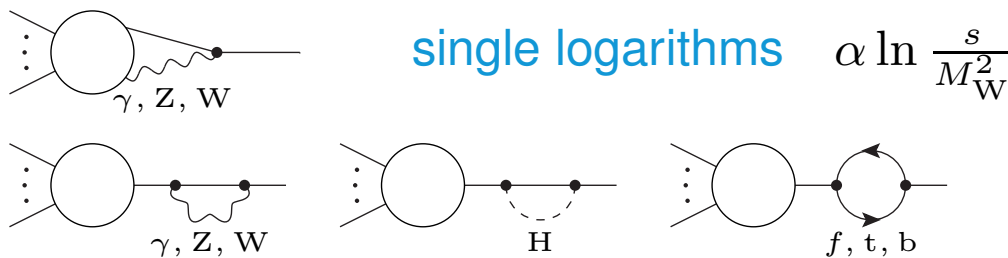
Large EW logarithms are of universal origin:

- infrared logarithms \Leftrightarrow external particles of the process
mass singularities in virtual corrections related to external lines

- ▶ soft and collinear virtual gauge bosons



- ▶ collinear or soft virtual gauge bosons, wave-function renormalization

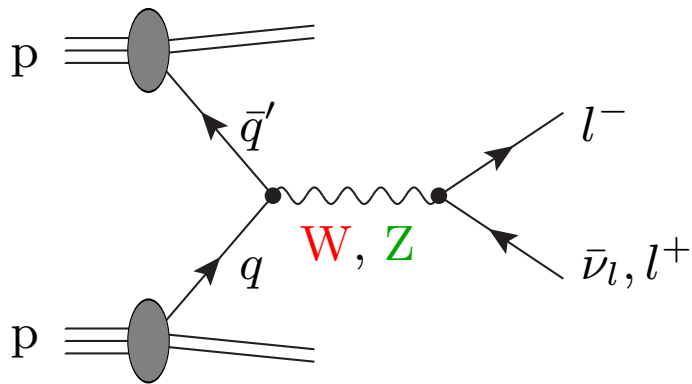


- ultraviolet logarithms \Leftrightarrow parameter renormalization at scale $M_W^2 \ll s$
 \Rightarrow running of electroweak couplings from M_W to \sqrt{s}
single logarithms $\alpha \ln \frac{s}{M_W^2}$

- have been studied by many people
 M. Ciafaloni, P. Ciafaloni, Comelli; Beccaria, Renard, Verzegnassi; Beenakker, Werthenbach; Denner, Pozzorini; Melles; Fadin, Lipatov, Martin; Jantzen, Kühn, Penin, Smirnov; Chiu, Fuhrer, Golf, Kelley, Manohar, ...
 - provide estimate for one-loop corrections at level of 5–10%
 - useful to estimate electroweak two-loop corrections
 - real corrections should be included
 - ▶ real photon radiation
 - ▶ real massive vector-boson radiation Baur '06
 ⇒ partial cancellation of enhanced corrections
 - **not reliable for processes with other sources of large contributions**
 e.g. large logarithms $\log(t/s) \sim 2 \log \theta$ for small θ not included (important for processes with large contributions in forward/backward directions)
 - at LHC often sizeable contributions from energies below 1 TeV
- ⇒ exact calculations of NLO EWRC preferable if possible

Example processes

Single gauge-boson production



large cross sections: $\sigma(W) = 30 \text{ nb}$
 $\sigma(Z) = 3.5 \text{ nb}$

Physics goals:

- M_Z → detector calibration by comparing with LEP1 result
- $\sin^2 \theta_{\text{eff}}^{\text{lept}}$ with $\delta \sin^2 \theta_{\text{eff}}^{\text{lept}} \sim 0.00014$ → comparison with results of LEP1 and SLC
- M_W → improvement to $\Delta M_W \sim 15 \text{ MeV}$ (7 MeV), strengthen EW precision tests
Besson et al. '08
- decay widths Γ_Z and Γ_W from M_{ll} or $M_{T, l\nu_l}$ tails
- search for Z' and W' at high M_{ll} or $M_{T, l\nu_l}$
- information on PDFs, determination of collider luminosity

QCD corrections to W/Z production

- NLO QCD corrections merged with QCD parton showers MC@NLO, POWHEG Frixione, Webber '02; Frixione, Nason, Oleari '07
- NNLO QCD corrections total cross section distributions Hamberg, v.Neerven, Matsuura '91; v.Neerven, Zijlstra '92; Harlander, Kilgore '02
Anastasiou et al. '03; Melnikov, Petriello '06
Catani et al. '09
- soft gluon resummation Balazs, Yuan '97; Ellis, Veseli '98
Landry et al. '02; Cao, Yuan '04

EW corrections to W/Z production

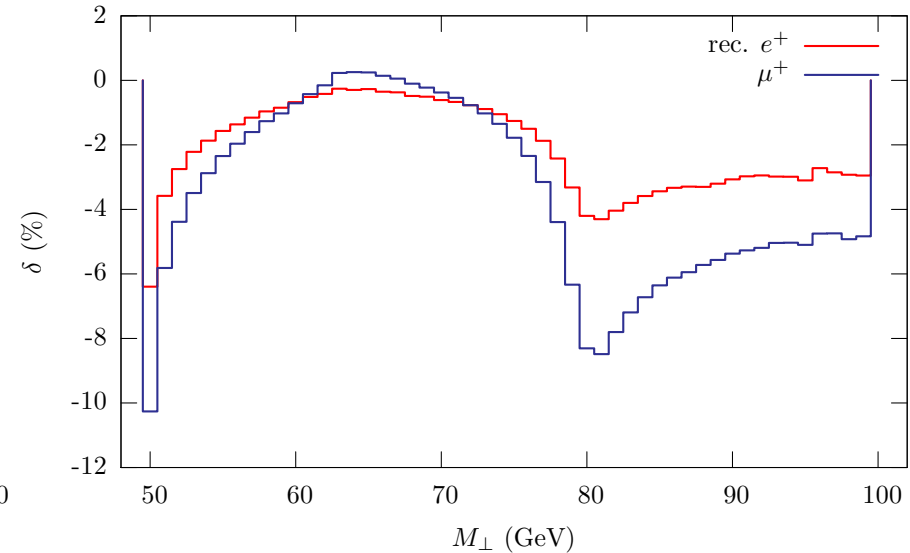
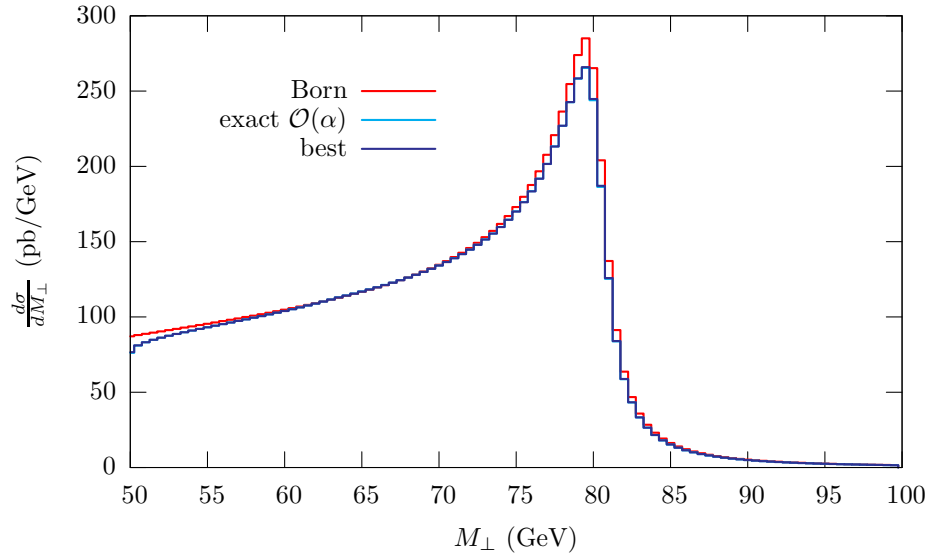
- NLO EW corrections to W production Baur, Keller, Wackerroth '98; Zykunov '01; Dittmaier, Krämer '02; Baur, Wackerroth '04
Arbuzov et al. '06; Carloni Calame et al. '06
- NLO EW corrections to Z production Baur, Keller, Sakumoto '97; Baur, Wackerroth '99
Brein, Hollik, Schappacher '99; Baur et al. '02
Zykunov '07; Arbuzov et al. '07
Carloni Calame et al. '07, Dittmaier, Huber '09
- multi-photon radiation via leading logs Baur, Stelzer '99; Carloni Calame et al. '03, '05
Placzek, Jadach '03; Breusing et al. '07
- photon-induced processes Dittmaier, Krämer '06; Arbuzov, Sadykov '07
Breusing et al. '07

transverse mass $M_{W,T} = \sqrt{2p_{\perp}^l p_{\perp}^{\nu} (1 - \cos \phi_{l\nu})}$

- **Jacobian peak at W mass** relatively insensitive to QCD ISR

Carloni Calame et al. '06

LHC14



- **final-state photon radiation distorts Breit–Wigner resonance** (kinematic effect!)

logarithmic corrections $\propto (\alpha/\pi) \log(M_V^2/m_l^2)$

\Rightarrow shift in extracted W mass: $\delta M_W \sim -170(60) \text{ MeV}$ for $W \rightarrow \mu\nu(e\nu)$

partial KLN cancellation for recombined electrons

- full EW $\mathcal{O}(\alpha)$ corrections: $\delta M_W \sim 10 \text{ MeV}$ Baur, Keller, Wackerroth. '99
- multiple final-state photon radiation: $\delta M_W \sim 10(2) \text{ MeV}$ Carloni Calame et al. '04

crucial for W and Z precision measurements but difficult beyond NLO

- simple first attempt: combination of soft-gluon resummation with final-state QED corrections (multiplicative) Cao, Yuan '04 (ResBos-A)
- additive or multiplicative combination of NLO QCD and EW correction
Balossini et al. '07, '09 (see also Bernaciak, Wackerath '12)

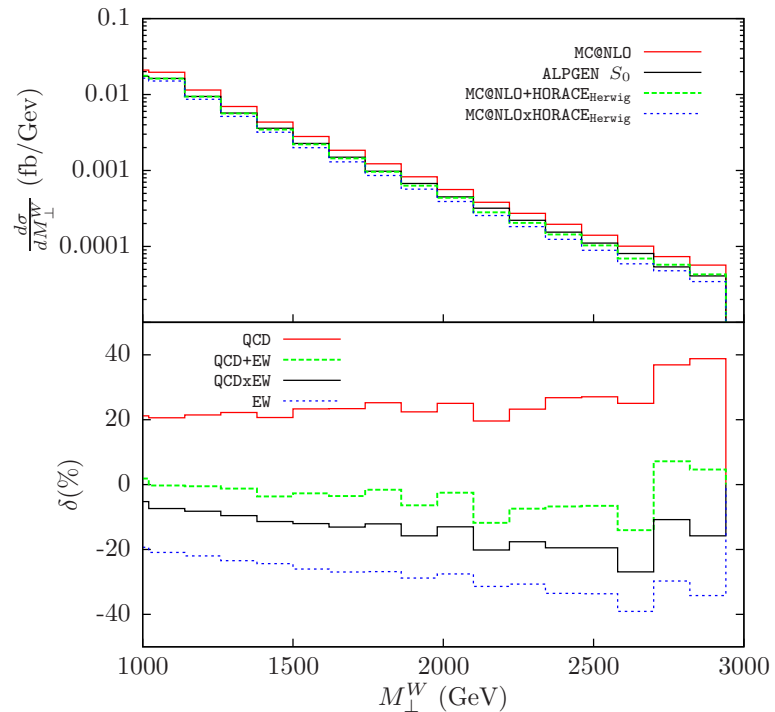
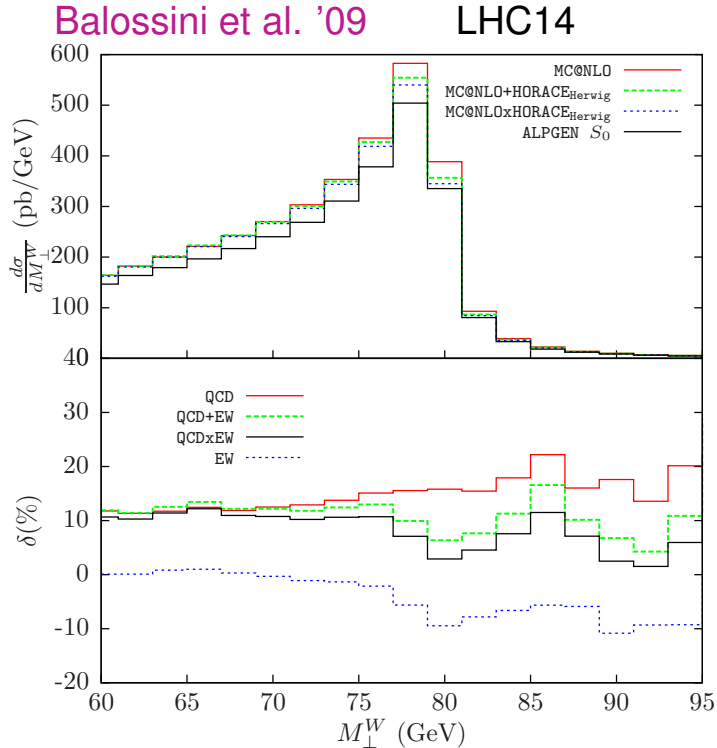
$$d\sigma_{\text{QCD} \oplus \text{EW}} = d\sigma_{\text{QCD}} + \{d\sigma_{\text{EW}} - d\sigma_{\text{LO}}\}_{\text{HERWIGPS}}$$

$$d\sigma_{\text{QCD} \otimes \text{EW}} = \left(1 + \frac{d\sigma_{\text{QCD}} - \{d\sigma_{\text{LO}}\}_{\text{HERWIGPS}}}{d\sigma_{\text{LO/NLO}}} \right) \{d\sigma_{\text{EW}}\}_{\text{HERWIGPS}}$$

EW = HORACE, QCD = MC@NLO Frixione, Webber '02

prescriptions agree at $\mathcal{O}(\alpha_s) + \mathcal{O}(\alpha)$ but differ at $\mathcal{O}(\alpha\alpha_s)$

- beyond additive approximation full two-loop $\mathcal{O}(\alpha\alpha_s)$ analysis needed
for Z production some corrections exist:
 - ▶ virtual $\mathcal{O}(\alpha\alpha_s)$ correction to quark–gauge-boson vertex Kotikov, Kühn, Veretin '07
 - ▶ virtual $\mathcal{O}(\alpha\alpha_s)$ of QED \times QCD type Kilgore, Sturm '11

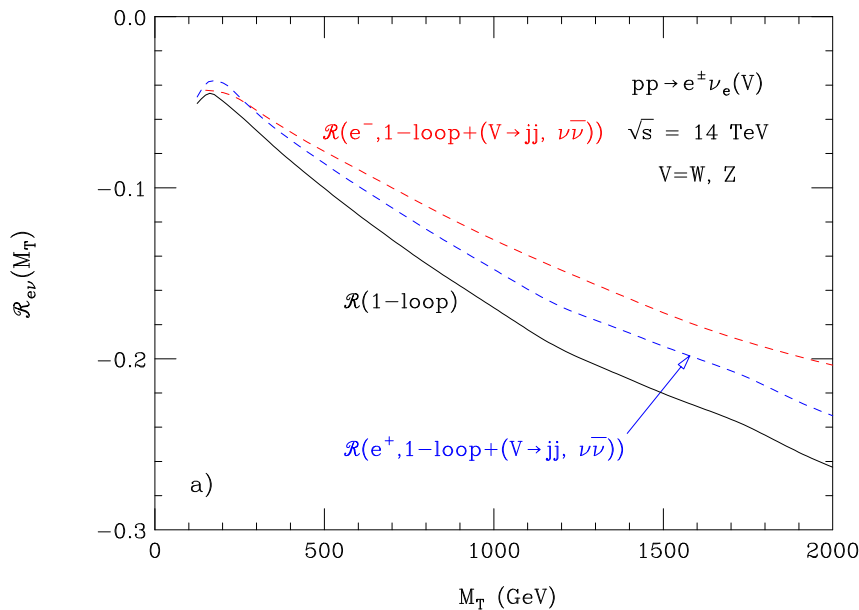


- corrections relative to LO+PS (ALPGEN S0)
- $M_{W,T} \sim M_W$: negative EW corrections compensate positive QCD corrections
EW corrections mandatory around Jacobian peak (-10%)
- $M_{W,T} \gg M_W$: large negative EW corrections (Sudakov logarithms)
cancel positive QCD corrections
- different ways of combining QCD and EW corrections differ at per-cent level
 $\Rightarrow \mathcal{O}(\alpha\alpha_s)$ calculation needed

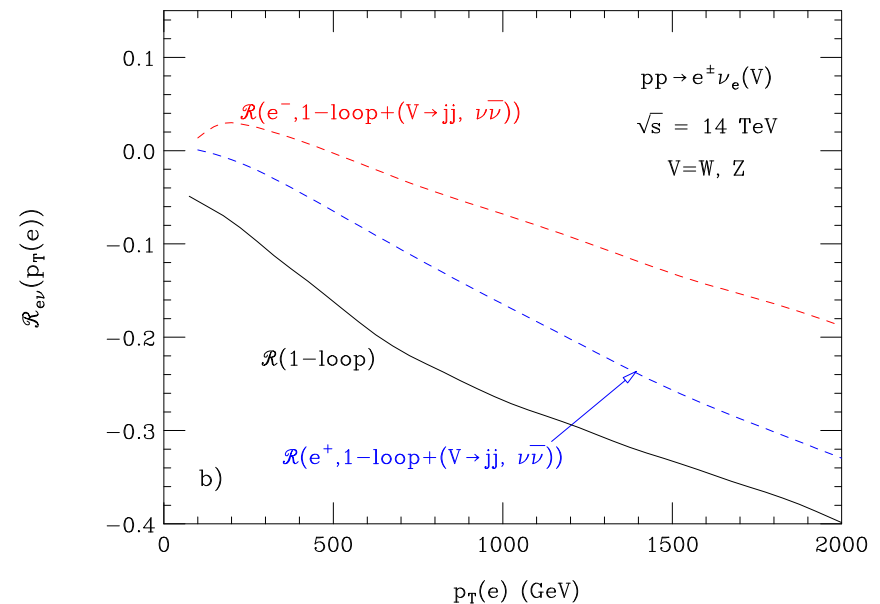
- Virtual EW corrections enhanced by large logarithms at high energy scales
- for realistic cuts real massive gauge-boson radiation partially cancels virtual EW corrections

Baur '06

transverse $e\nu$ mass

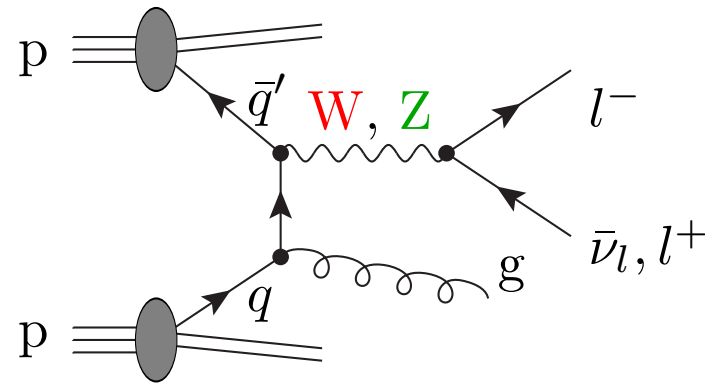
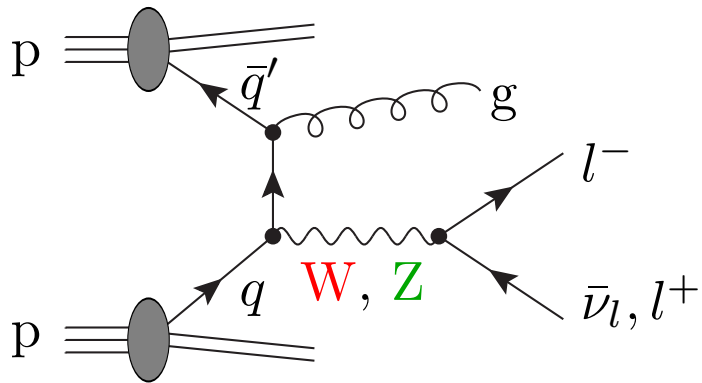


transverse electron momentum



- $M_T(e\nu) = 2 \text{ TeV}$: reduction of corrections from -26% to $-23\% / -22\%$
- $p_T(e) = 1 \text{ TeV}$: reduction of corrections from -28% to $-17\% / -7\%$

Gauge-boson plus jet production



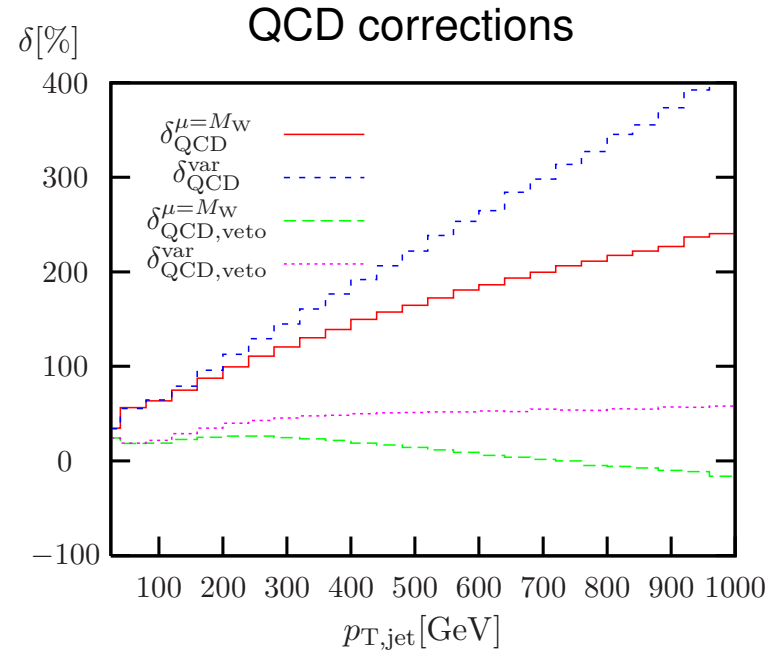
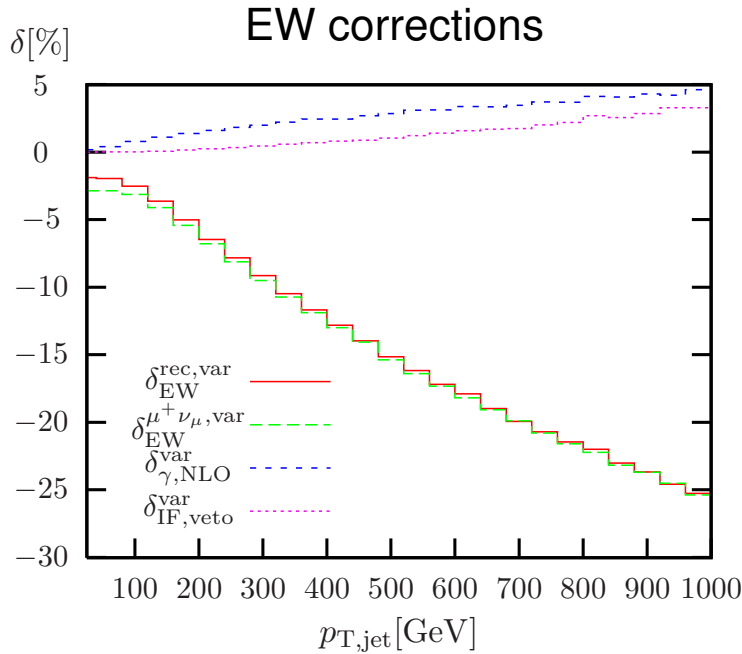
- important contribution to single V production
 \Rightarrow measurement of M_V, Γ_V , electroweak mixing angle $\sin^2 \theta_{\text{eff}}^{\text{lept}}$
- tests of jet dynamics in QCD
- constraints on parton distribution functions (PDFs)
- source of high-energy leptons and/or missing transverse momentum
 \Rightarrow background to new physics

EW corrections

- $pp \rightarrow V + \text{jet} + X$ ($V = \gamma, Z$)
 - ▶ weak $\mathcal{O}(\alpha)$ correction (stable Z) Maina, Moretti, Ross '04
 $\delta_{\text{weak}} \sim -(5-15)\%$ for $p_T \lesssim 500 \text{ GeV}$
 - ▶ (NLO + NNLL) EW corrections (stable Z) Kühn, Kulesza, Pozzorini, Schulze '04, '05
 - ▶ EW and QCD NLO corrections for $pp \rightarrow l^+l^- + \text{jet} + X$,
 i.e. $pp \rightarrow Z + \text{jet} + X$ including leptonic decays Denner, Dittmaier, Kasprzik, Mück '11

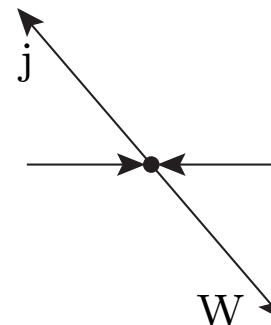
- $pp \rightarrow W + \text{jet} + X$
 - ▶ EW corrections for stable W: Kühn et al. '07; Hollik, Kasprzik, Kniehl '07
 $\delta_{\text{weak}} \sim -30\%$ for $p_T \sim 2000 \text{ GeV}$
photo production appreciably contributes to relative corrections (+10%@2 TeV)
 Hollik et al. '07
 - ▶ EW and QCD NLO corrections for $pp \rightarrow l\nu + \text{jet} + X$,
 i.e. $pp \rightarrow W + \text{jet} + X$ including leptonic decays Denner, Dittmaier, Kasprzik, Mück '10

Denner, Dittmaier, Kasprzik, Mück '11

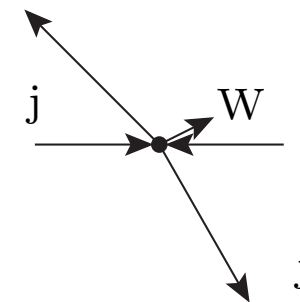


- large electroweak corrections for high p_T Sudakov logarithms
- 5% photon-induced corrections at 1 TeV
- huge QCD corrections owing to new subprocess $pp \rightarrow 2 \text{ jets} + W$ with two opposite hard jets and soft W
veto on 2nd jet reduces corrections considerably

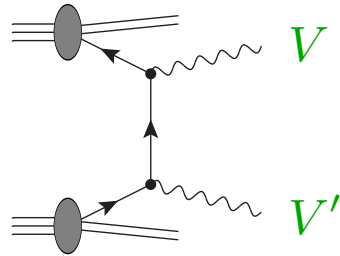
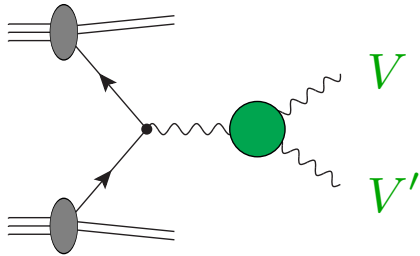
LO process



new NLO process



Gauge-boson pair production



$$V, V' = \gamma, Z, W^\pm$$

$$\sigma(WW) \sim 100 \text{ fb}$$

$$\sigma(W^\pm Z) \sim 30/20 \text{ fb}$$

$$\sigma(ZZ) \sim 15 \text{ fb}$$

Physics issues:

- **triple-gauge-boson couplings** at high momentum transfer
- dynamics of **longitudinal massive gauge bosons at high energies**
 $W_L, Z_L \sim$ Goldstone bosons \rightarrow window to scalar sector
- **important class of background processes** to many searches
 (e.g. $H \rightarrow VV \rightarrow 4f$, supersymmetry)

NLO QCD corrections available for full process including leptonic decays

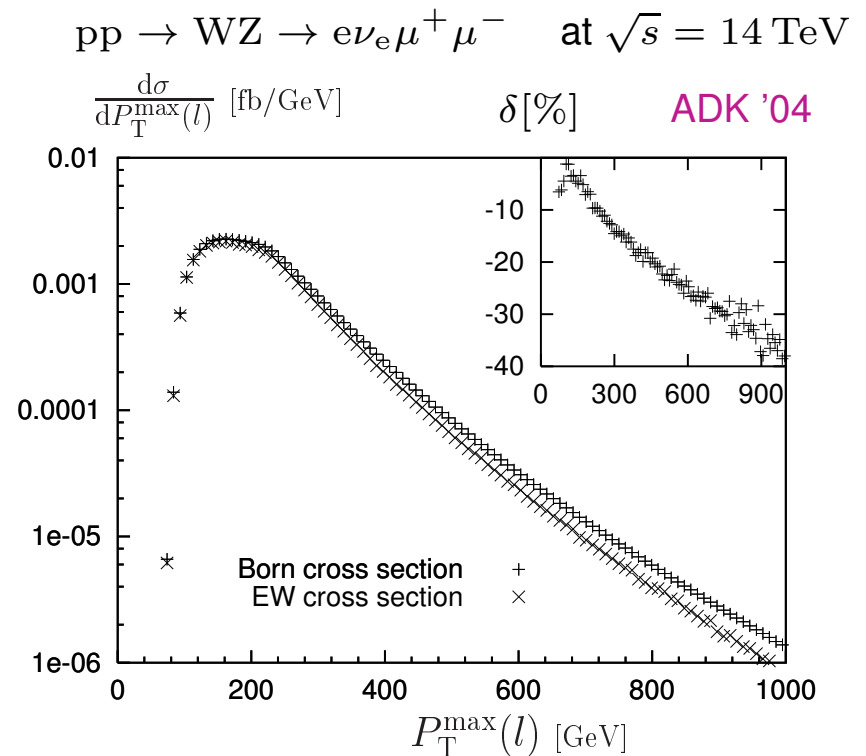
Dixon, Kunszt, Signer '99, Campbell, Ellis '99; De Florian, Signer '00

- $pp(\rightarrow W\gamma) \rightarrow l\bar{\nu}\gamma + X$ Accomando, Denner, Pozzorini '01; Accomando, Denner, Meier '05
 $\mathcal{O}(\alpha)$ correction in pole approximation
 $\hookrightarrow \delta \sim -10\% (-27\%)$ for $p_{T,\gamma} \gtrsim 250 \text{ GeV} (700 \text{ GeV})$
- $pp \rightarrow Z\gamma + X$ Hollik, Meier '04 and $pp(\rightarrow Z\gamma) \rightarrow ll\gamma + X$ Accomando, Denner, Meier '05
 complete $\mathcal{O}(\alpha)$ correction for on-shell Z bosons in pole approximation
 $\hookrightarrow \delta \sim -10\%$ for $M_{\gamma Z}$ distribution
- $pp(\rightarrow WW, WZ, ZZ) \rightarrow 4 \text{ leptons} + X$

Accomando, Denner, Pozzorini '01
 Accomando, Denner, Kaiser '04

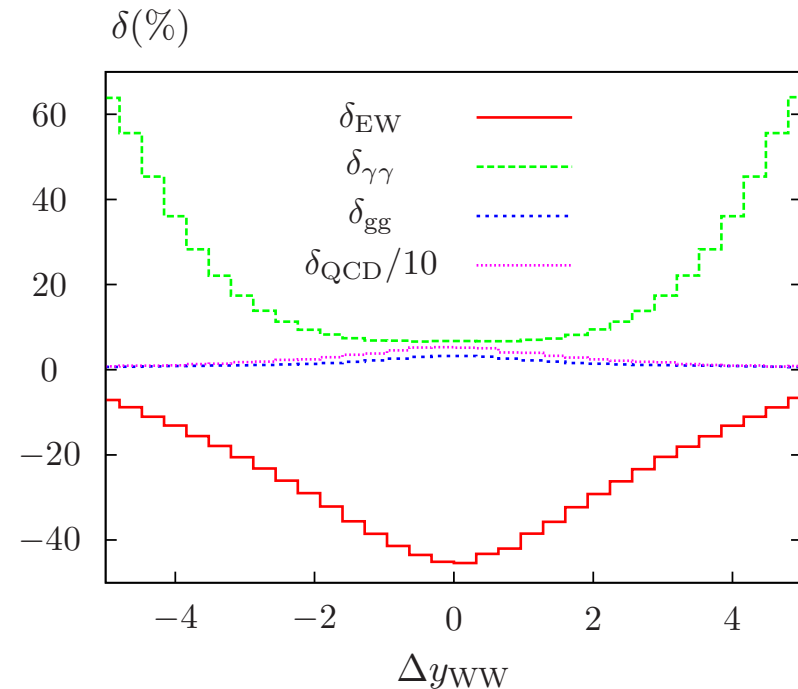
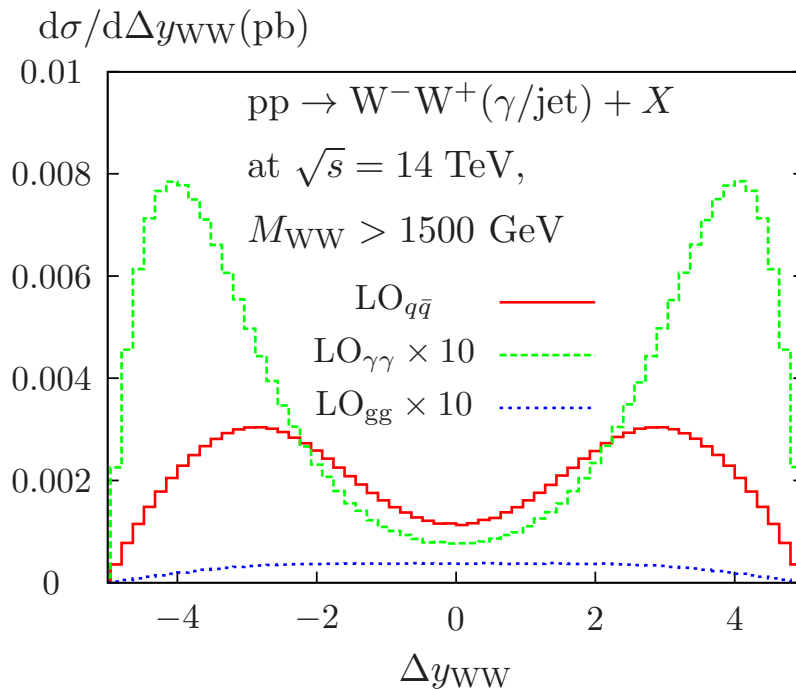
$\mathcal{O}(\alpha)$ correction in high-energy
 and pole approximations

large negative EW corrections
 (Sudakov logarithms)
for large energy scales



- $pp \rightarrow WW, WZ, ZZ + X$ (on-shell gauge bosons) Bierweiler, Kasprzik, Kühn, Uccirati '12 including
 - ▶ complete EW and QCD NLO corrections
 - ▶ photon- and gluon-induced processes: $\gamma\gamma \rightarrow WW, gg \rightarrow WW$
 - ▶ radiation of massive vector bosons: $qq \rightarrow WWV$

distribution in rapidity difference of W bosons (sensitive to anomalous couplings)



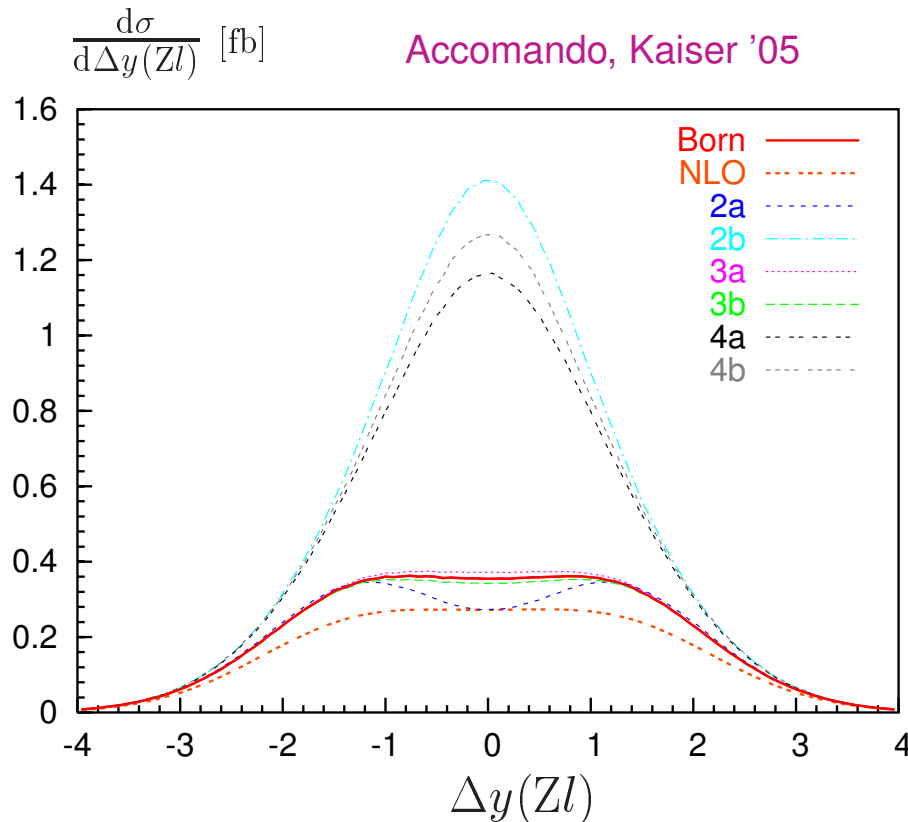
dramatic distortion of distribution at level of 50% (mimics anomalous couplings)

$pp \rightarrow WZ \rightarrow l\nu_l l' \bar{l}'$:

distribution in rapidity difference of Z boson and lepton from W decay $\Delta y(Zl)$

NLO = NLO electroweak: $\sim -20\%$

2a/2b: $\Delta g_1^Z = \pm 0.02$, 3a/3b: $\Delta \kappa_\gamma = \pm 0.04$, 4a/4b: $\lambda = \pm 0.02$



Conclusions

NLO corrections

- important for reliable predictions of cross sections and distributions
- typically some 10%, but may be strongly enhanced
- rapid progress in calculational techniques during recent years
 - ▶ successes of unitarity-based techniques (first 2 → 5 results)
 - ▶ improvement of diagrammatic techniques
- state of the art:
 - 2 → 4 calculations, first 2 → 5 calculations available

EW NLO corrections

- typically at level of few % to 10%
 - ↔ important for precise measurements
- strongly enhanced in some kinematic regions
(high energy scales, resonance regions)