

# The Standard Model of Particle Physics

## Lecture IV

The Standard Model in the LHC era

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Maria Laach School, Bautzen, September 2011

# Outline of Lecture IV

- Standard Model processes as background to new physics:
  - new physics searches at hadron colliders: structure of hadronic processes, most important building blocks;
  - theoretical prediction dominated by QCD effects;
  - high accuracy in theoretical predictions needed: challenges;
  - recent developments and existing tools;
  - milestone examples.

# Beyond Higgs boson physics ...

Building on solid SM ground, we can start exploring beyond SM scenarios in as much generality as possible, looking for most distinctive patterns and signatures of various realizations of EWSB.

↪ “Signatures of new physics at the LHC” (SLAC)

Typical signatures will have: jets +  $\cancel{E}_T$  (+leptons)

Main Standard Model irreducible/reducible backgrounds:

→  $W/Z + n$ -jets

→  $W/Z + b$ -jets

→  $t\bar{t}$ +jets

→ ...

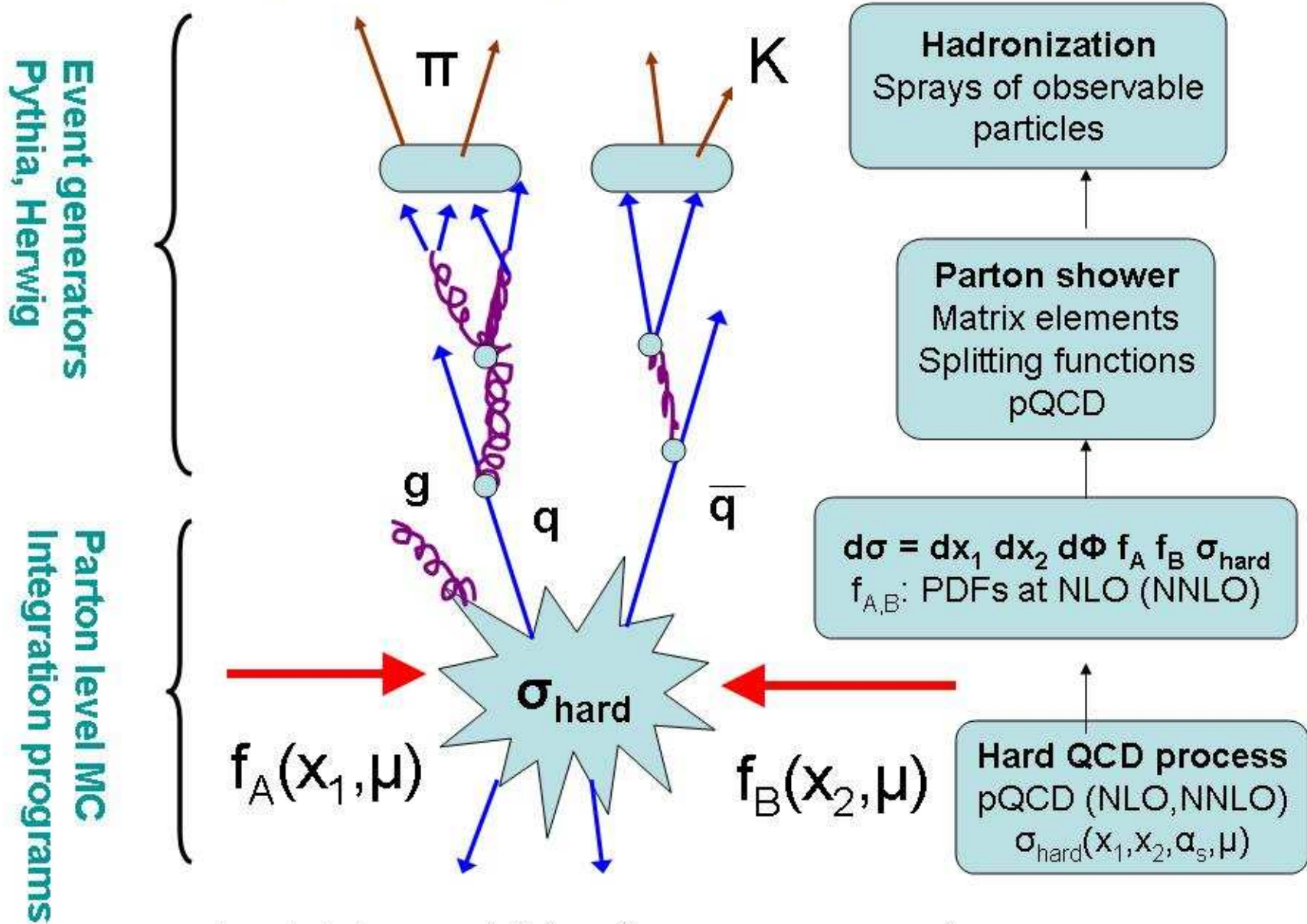
all characterized by: large multiplicity and many massive particles.

A reliable quantitative description of strong dynamics in high energy collisions remains as a crucial technical challenge

which has been

largely faced during the last decade.

# Anatomy of a QCD prediction at hadron colliders



+ underlying event, interactions among remnants

# Schematically ...

The hard cross section is calculated perturbatively

$$\hat{\sigma}(ij \rightarrow X) = \alpha_s^k \sum_{m=0}^n \hat{\sigma}_{ij}^{(m)} \alpha_s^m$$

n=0 : **Leading Order** (LO), or tree level or Born level

n=1 : **Next to Leading Order** (NLO), include  $O(\alpha_s)$  corrections

.....

and convoluted with initial state parton densities at the same order.

Renormalization and factorization scale dependence left at any fixed order.

Setting  $\boxed{\mu_R = \mu_F = \mu}$  :

$$\sigma(pp, p\bar{p} \rightarrow X) = \sum_{ij} \int dx_1 dx_2 f_i^p(x_1, \mu) f_j^{p,\bar{p}}(x_2, \mu) \sum_{m=0}^n \hat{\sigma}_{ij}^{(m)}(\mu, Q^2) \alpha_s^{m+k}(\mu)$$

Systematic theoretical error from:

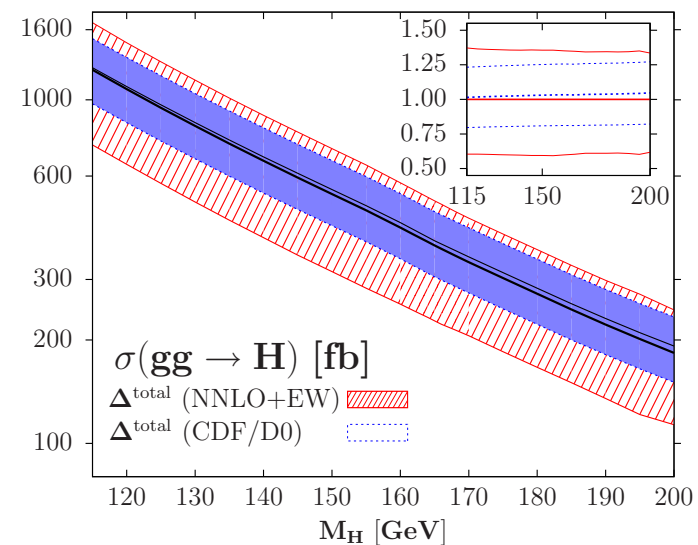
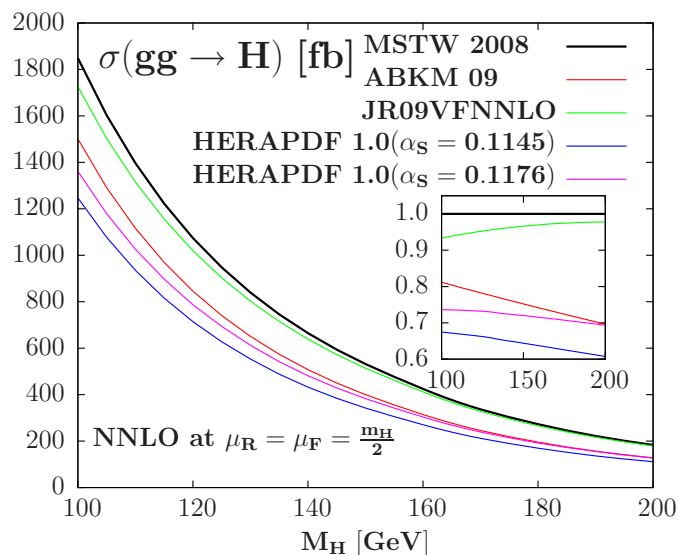
- ▷ PDF and  $\alpha_s(\mu)$ ;
- ▷ left over scale dependence;
- ▷ input parameters.

# Systematic error from PDFs: need care ...

Several PDF sets (CTEQ, MSTW, NNPDF, ...) allow to estimate the error from  $\alpha_s$  and error obtained by varying the inputs used in the PDF fit within their experimental error.

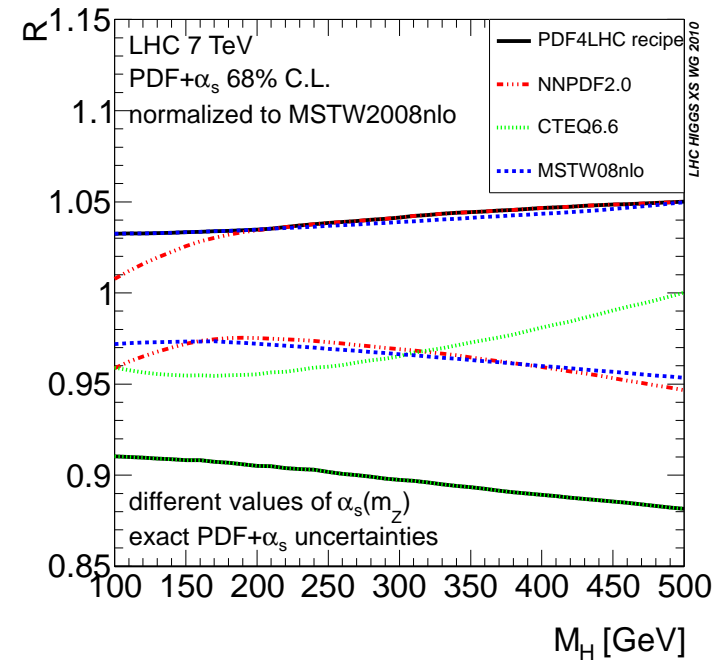
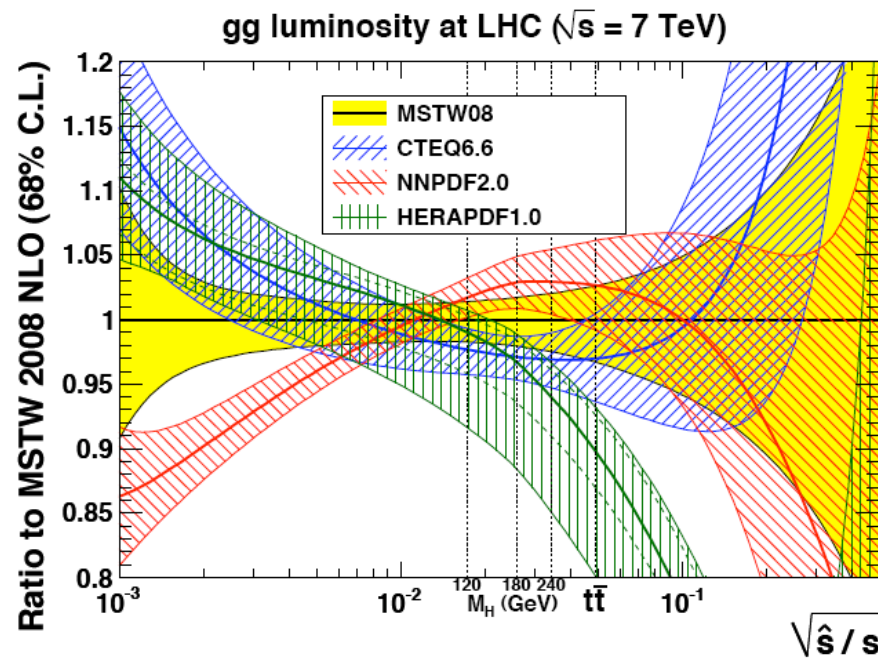
However: results obtained using different sets of PDF differ by much more than the respective internal errors  $\rightarrow$  difference from parametrization

Example: Tevatron bound has been questioned with the claim that the error from PDF's has been largely underestimated



(Baglio, Djouadi, Ferrag, Godbole, arXiv:1101.1832)

# PDF4LHC: problem carefully studied for LHC physics



(Forte, Huston, Mazumdar, Thorne, Vicini, arXiv:1101.0593)

- NLO: use sets that perform a global fit to all available collider data: CTEQ(6.6), MSTW(2008), NNPDF(2.0). Estimate the error from PDF using the envelope prescription.
- NNLO: use MSTW(2008), normalized to a more conservative error i.e. multiplied by (NLO envelope error/NLO MSTW2008 error).

# Hard cross sections: pushing the loop order, why?

- **Stability and predictivity of theoretical results**, since less sensitivity to unphysical renormalization/factorization scales. First reliable normalization of total cross-sections and distributions.
- **Physics richness**: more channels and more partons in final state, i.e. more structure to better model (in perturbative region):
  - differential cross-sections, exclusive observables;
  - jet formation/merging and hadronization;
  - initial state radiation.
- **First step towards matching with** algorithms that resum particular sets of large corrections in the perturbative expansion: **resummed calculations, parton shower Monte Carlo** programs.



# Main challenges ...

- **Multiplicity** and **Massiveness** of final state: complex events leads to complex calculations. For a  $2 \rightarrow N$  process **one needs**:
  - calculation of the  $2 \rightarrow N + 1$  (NLO) or  $2 \rightarrow N + 2$  real corrections;
  - calculation of the 1-loop (NLO) or 2-loop (NNLO)  $2 \rightarrow N$  virtual corrections.
- **Flexibility** of NLO/NNLO calculations via **Automation**:
  - algorithms suitable for automation are more efficient and force the adoption of standards;
  - faster response to experimental needs (think to the impact of projects like MCFM).
- **Matching to Parton Shower** Monte Carlos at NLO.
  - instead of correcting NLO parton level calculation to match the hadron level, shower with NLO precision!

# NLO: challenges have largely been faced and enormous progress has been made

- several independent codes based on traditional FD's approach
- several NLO processes collected and viable in MFCM ( $\rightarrow$  interfaced with FROOT) [Campbell, Ellis]
- Enormous progress towards automation:
  - $\rightarrow$  Virtual corrections: new techniques based on unitarity methods and recursion relations
    - $\triangleright$  BlackHat [Berger, Bern, Dixon, Febres Cordero, Forde, Ita, Kosower, Maitre]
    - $\triangleright$  Rocket [Ellis, Giele, Kunszt, Melnikov, Zanderighi]
    - $\triangleright$  HELAC+CutTools, Samurai [Bevilacqua, Czakon, van Harmeren, Papadopoulos, Pittau, Worek; Mastrolia, Ossola, Reiter, Tramontano]
  - $\rightarrow$  Real corrections: based on Catani-Seymour Dipole subtraction or FKS subtraction
    - $\triangleright$  Sherpa [Gleisberg, Krauss]
    - $\triangleright$  Madgraph (AutoDipole) [Hasegawa, Moch, Uwer]
    - $\triangleright$  Madgraph (MadDipole) [Frederix, Gehrmann, Greiner]
    - $\triangleright$  Madgraph (MadFKS) [Frederix, Frixione, Maltoni, Stelzer]

- virtual+real:
  - ▷ MadLoop+MadFKS [Hirschi, Frederix, Frixione, Garzelli, Maltoni, Pittau]
- interface to parton shower well advanced:
  - ▷ MC@NLO [Frixione, Webber, Nason, Frederix, Maltoni, Stelzer]
  - ▷ POWHEG [Nason, Oleari, Alioli, Re]

## When is NLO not enough?

- When **NLO corrections** are **large**, to tests the convergence of the perturbative expansion. This may happen when:
  - processes involve multiple scales, leading to large logarithms of the ratio(s) of scales;
  - new parton level subprocesses first appear at NLO;
  - new dynamics first appear at NLO;
  - ...
- When truly **high precision** is needed (very often the case!).
- When a really **reliable error estimate** is needed.

## Some guiding principles:

- reduce the dependence on unphysical scales (renorm./fact. scale);
- have the perturbative expansion of physical observables (inclusive  $\sigma$ , distributions, ...) to show a well behaved convergence.

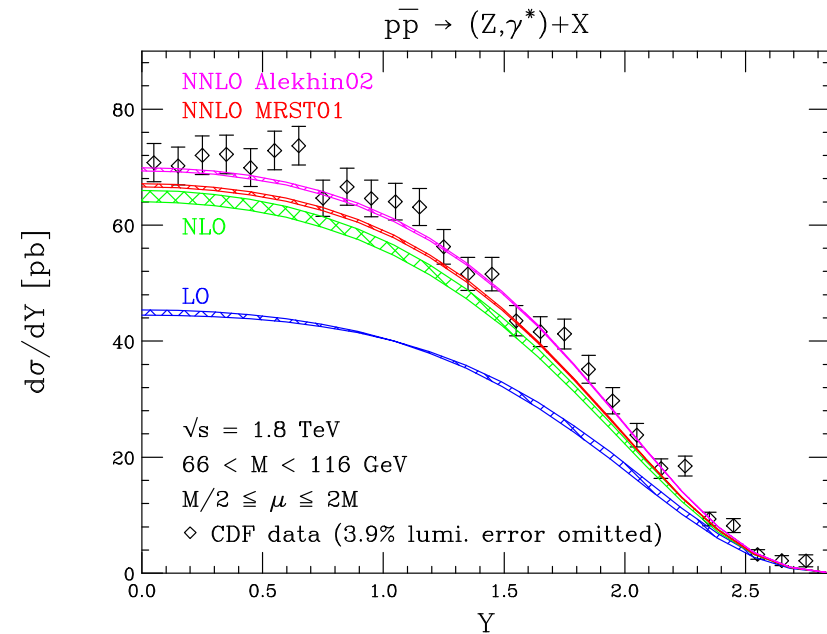
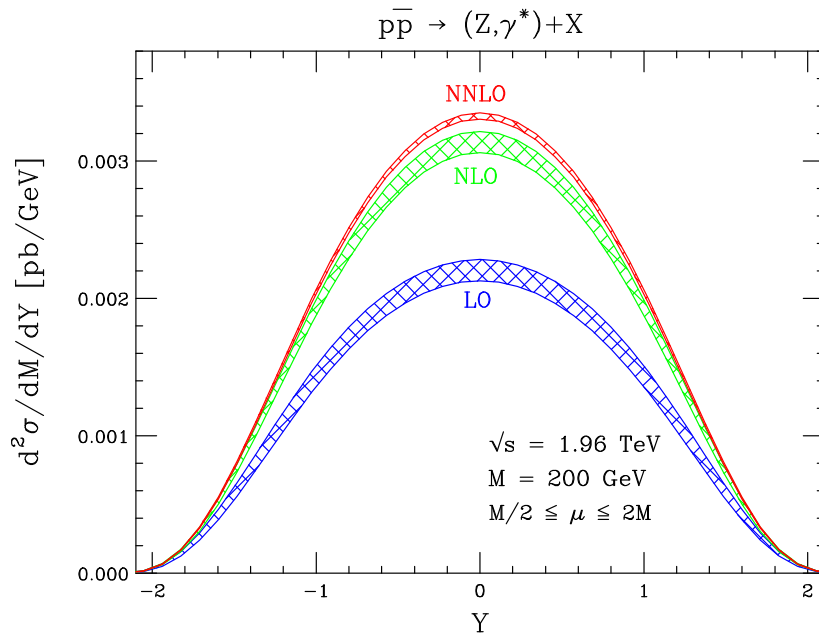
## Several possible steps:

- add enough higher order corrections (NLO, NNLO) till: scale dependence improves, no large next order corrections expected;
- look for recurrent large contributions that may spoil convergence;
- find the best expansion parameter ( $\alpha_s$ ,  $\alpha_s$  times large logarithms, ...);
- using scaling properties, resum large scale dependent corrections;
- find the best choice of unphysical scales to avoid generating large logarithmic corrections at all orders;
- study the effect of cuts and vetos.

Interesting to look at some examples

## Ex. 1: $W/Z$ production at the Tevatron, testing PDF's at NNLO.

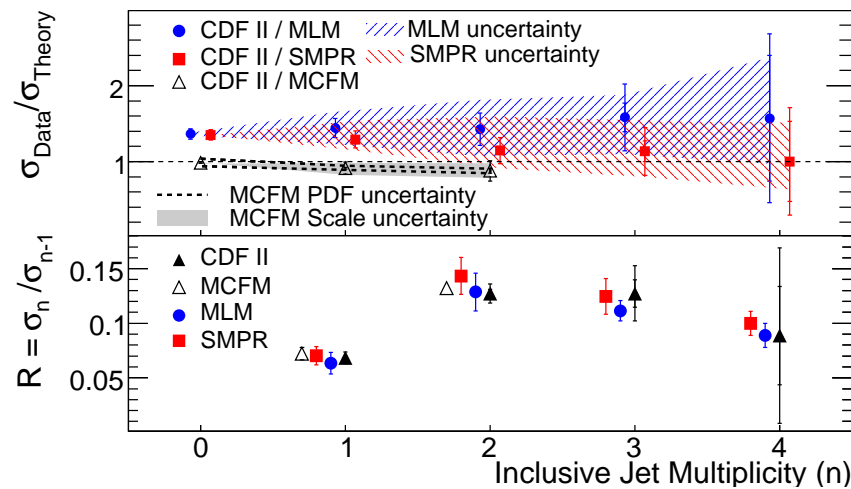
Rapidity distributions of the  $Z$  boson calculated at NNLO:



(C. Anastasiou, L. Dixon, K. Melnikov, F. Petriello, PRL 91 (2003) 182002)

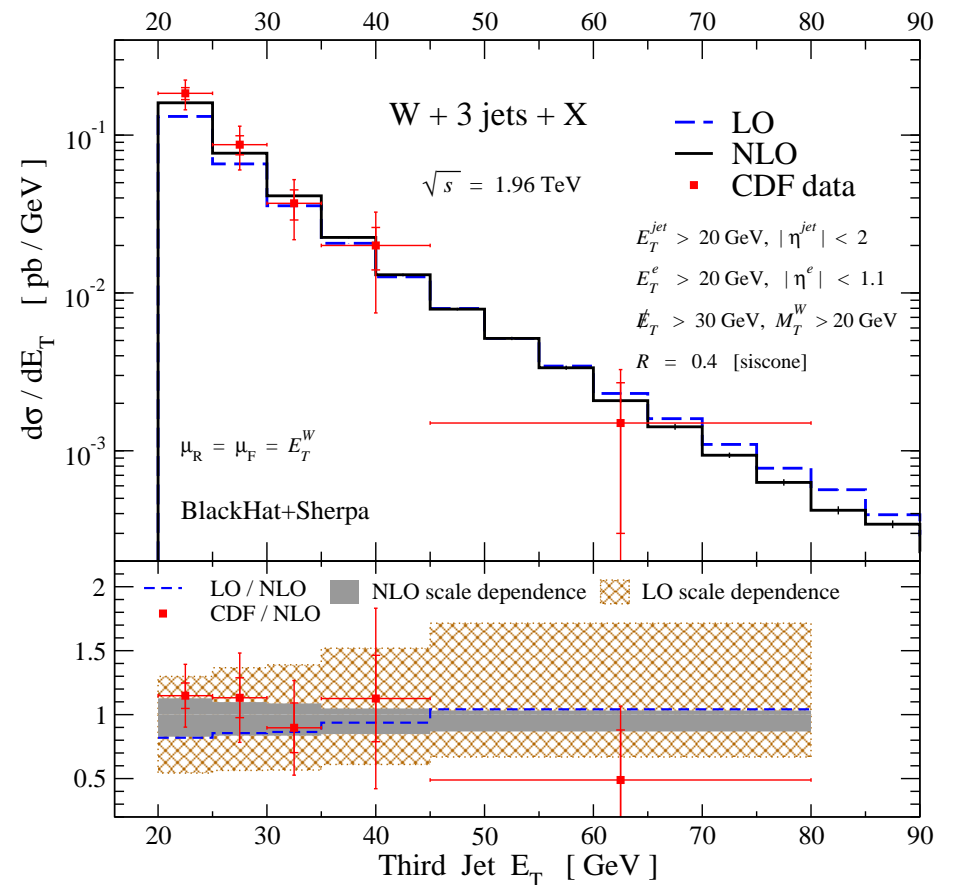
- $W/Z$  production processes are standard candles at hadron colliders.
- Testing NNLO PDF's: parton-parton luminosity monitor, detector calibration.

## Ex. 2: $W$ +jets production at the Tevatron, where progress has been most impressive!



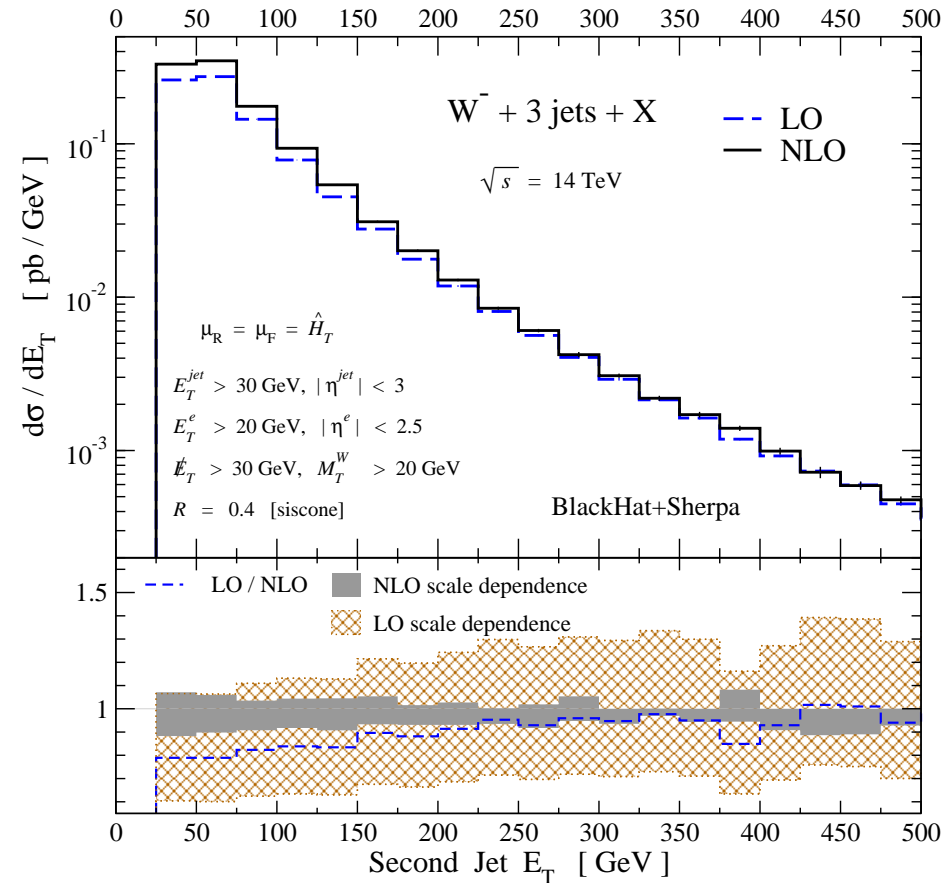
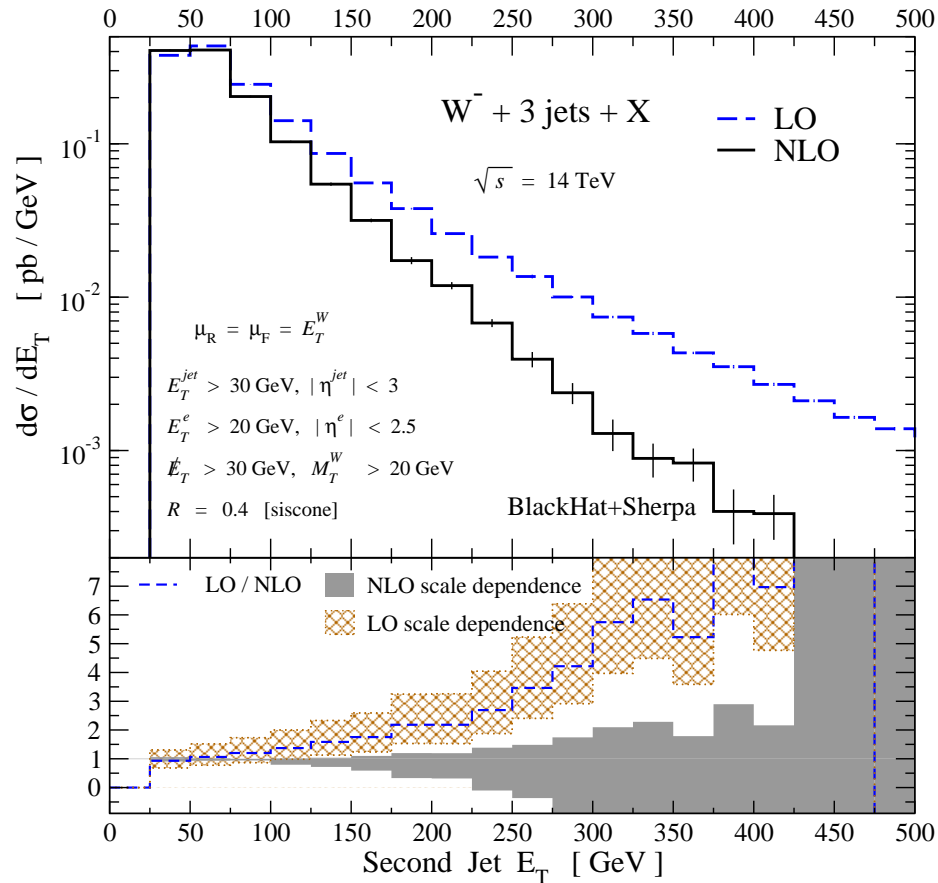
(CDF collaboration, arXiv:0711.4044)

- much reduced systematics at NLC
- only up to  $W + 2j$  available in '07
- today  $W + 3j$  and  $W + 4j$  available at NLO.



(Berger et al., arXiv:0907.1984)

# Best scale choice only possible with NLO wisdom ...



(Berger, Bern, Dixon, Febres Cordero, Forde, Gleisberg, Kosower, Maitre, arXiv:0907.1984)

“Wrong” scale choice leads to enhanced unphysical instabilities

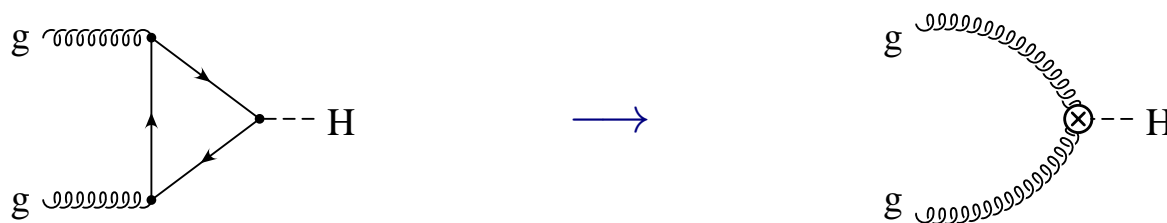


Ex. 3:  $gg \rightarrow H$ , main production mode (with  $H \rightarrow \gamma\gamma, W^+W^-, ZZ$ )  
 ... large K-factors, scale dependence, resummations, and more.

NLO QCD corrections calculated exactly and in the  $m_t \rightarrow \infty$  limit:  
 perfect agreement even for  $M_H \gg m_t$ .



Dominant soft dynamics do not resolve the Higgs boson coupling to gluons

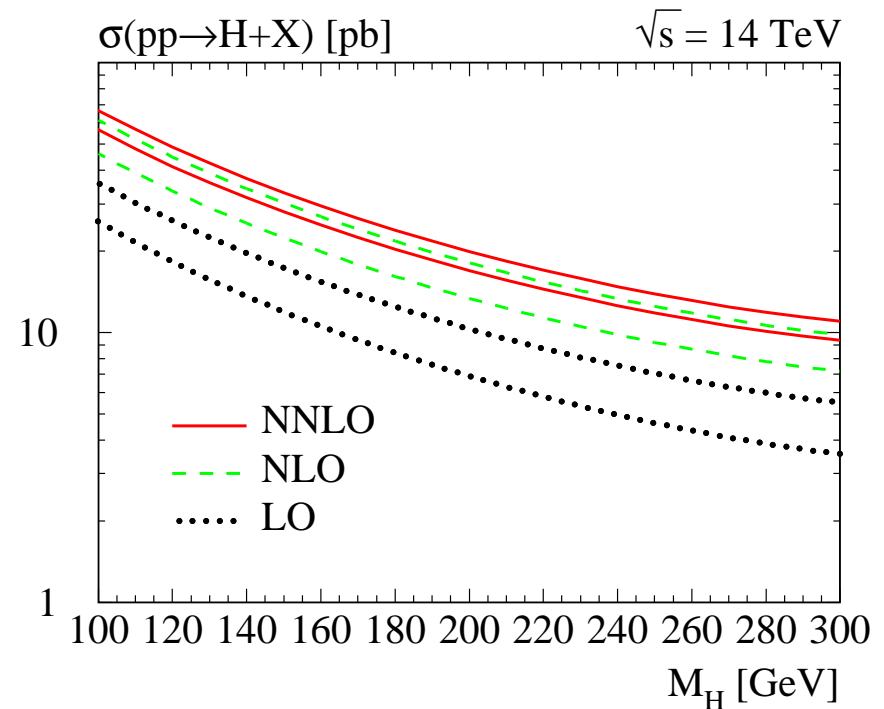
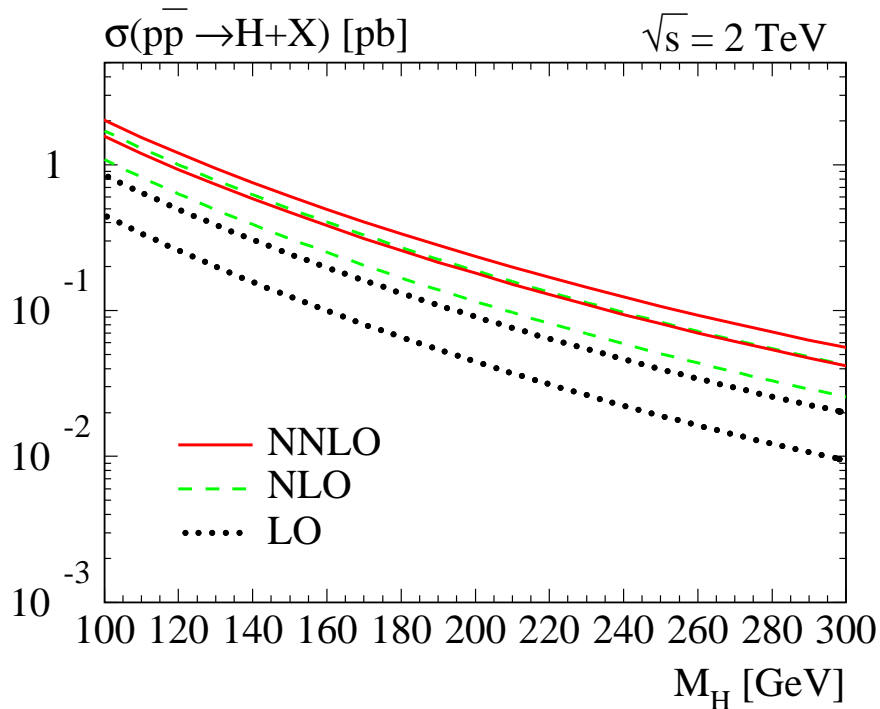


$$\mathcal{L}_{eff} = \frac{H}{4v} C(\alpha_s) G^{a\mu\nu} G_{\mu\nu}^a$$

where, including NLO and NNLO QCD corrections:

$$C(\alpha_s) = \frac{1}{3} \frac{\alpha_s}{\pi} \left[ 1 + c_1 \frac{\alpha_s}{\pi} + c_2 \left( \frac{\alpha_s}{\pi} \right)^2 + \dots \right]$$

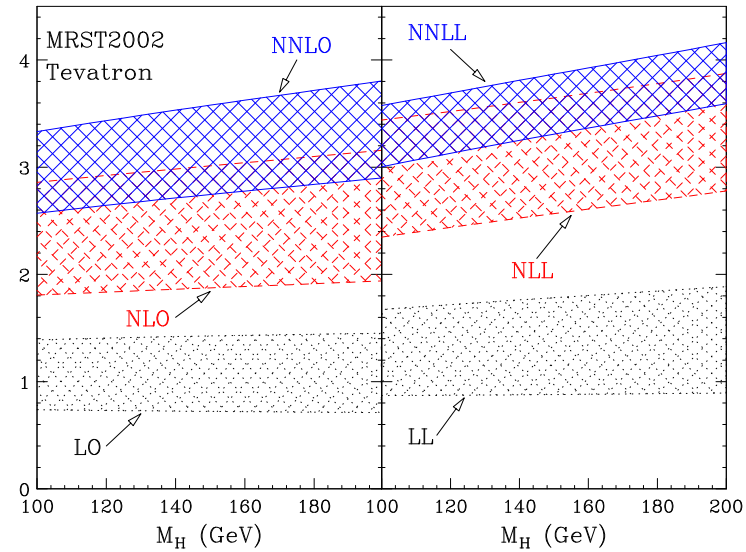
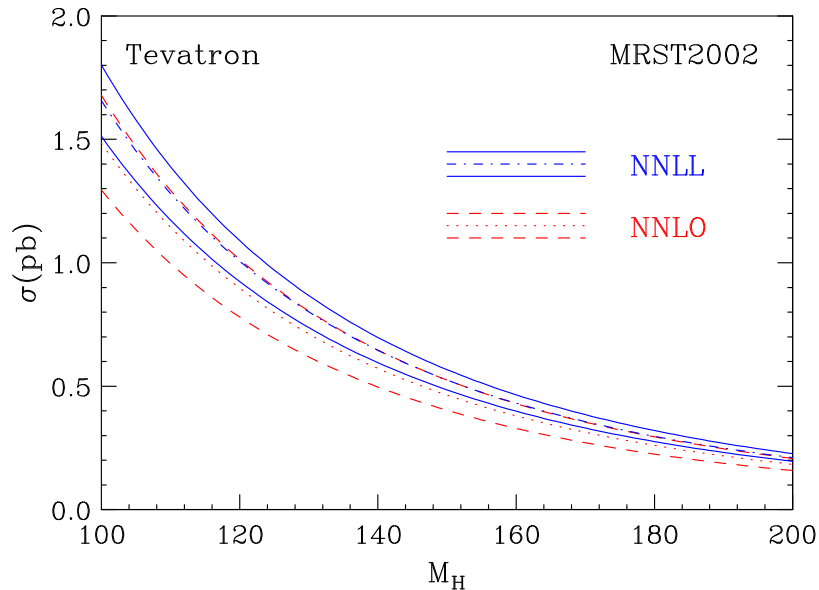
## Fixed order NNLO:



[Harlander, Kilgore (02)]

- very large corrections in going LO  $\rightarrow$  NLO (K=1.7-1.9)  $\rightarrow$  NNLO (K=2-2.2);
- perturbative convergence LO  $\rightarrow$  NLO (70%)  $\rightarrow$  NNLO (30%):  
residual 15% theoretical uncertainty.
- Tevatron case: still some tension.

# Resumming effects of soft radiation ...



[Catani, de Florian, Grazzini, Nason(03)]

Theoretical uncertainty reduced to:

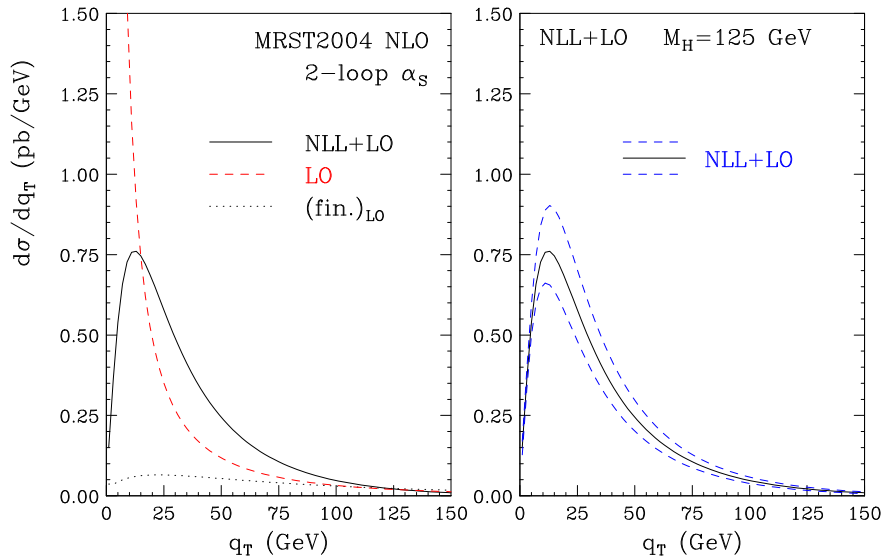
→  $\simeq 10\%$  perturbative uncertainty, including the  $m_t \rightarrow \infty$  approximation.

→  $\simeq 10\%$  (estimated) from NNLO PDF's (now existing!).

But ... let us remember that: going from MRST2002 to MSTW2008 greatly affected the Tevatron/LHC cross section: from  $9\%/30\%$  ( $M_H = 115$  GeV) to  $-9\%/+9\%$  ( $M_H = 200/300$  GeV) !

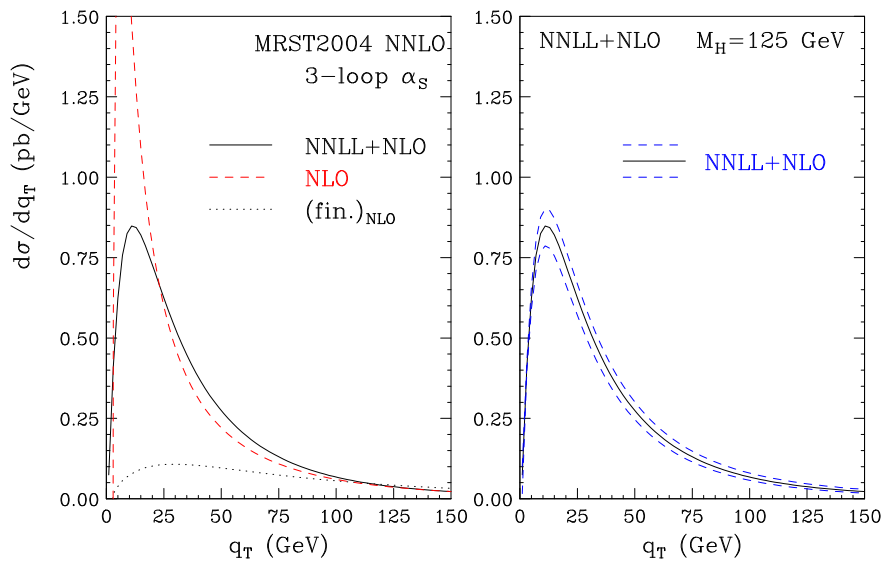
[De Florian, Grazzini (09)]

# Resumming effects of soft radiation for $q_T^H$ spectrum ...



large  $q_T \xrightarrow{q_T > M_H}$   
perturbative expansion in  $\alpha_s(\mu)$

small  $q_T \xrightarrow{q_T \ll M_H}$   
need to resum large  $\ln(M_H^2/q_T^2)$



residual uncertainty:

LO-NLL: 15-20%

NLO-NNLL: 8-20%

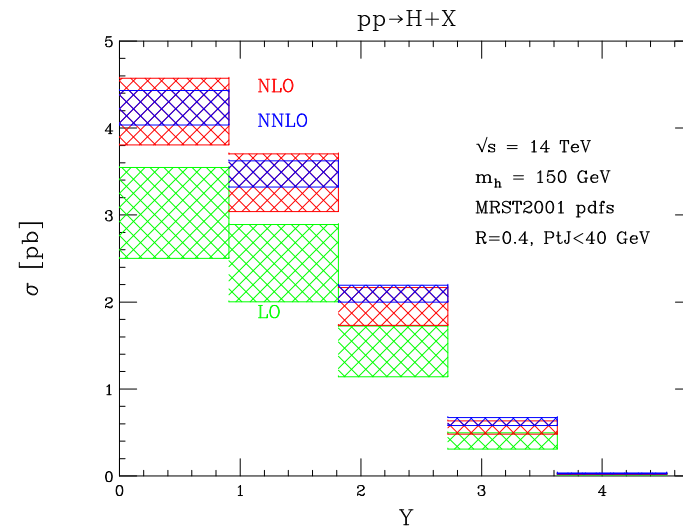
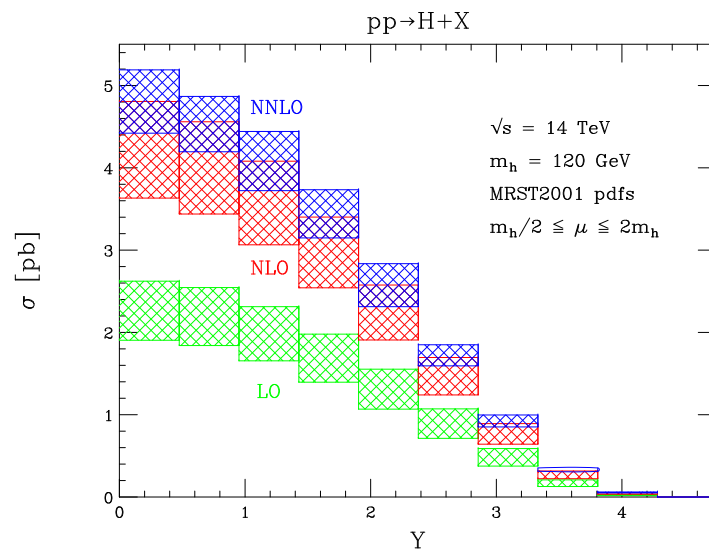
# Exclusive NNLO results: $gg \rightarrow H, H \rightarrow \gamma\gamma, WW, ZZ$

Extension of (IR safe) subtraction method to NNLO

→ HNNLO [Catani, Grazzini (05)]

→ FEHiP [Anastasiou, Melnikov, Petriello (05)]

Essential tools to reliably implement experimental cuts/vetos.

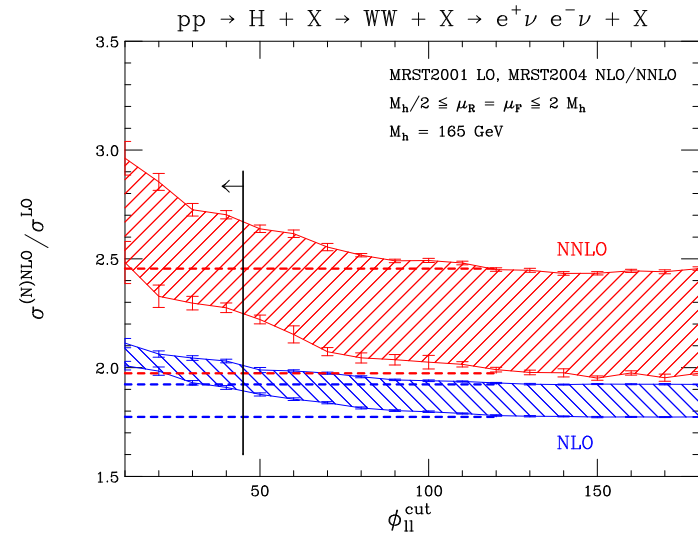
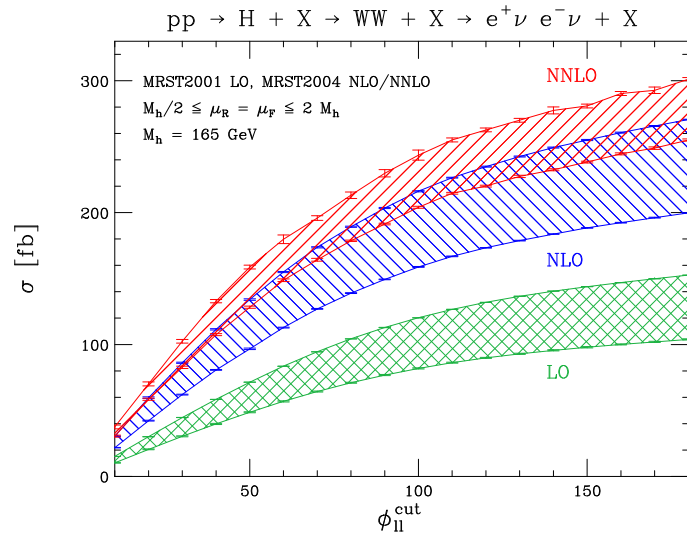
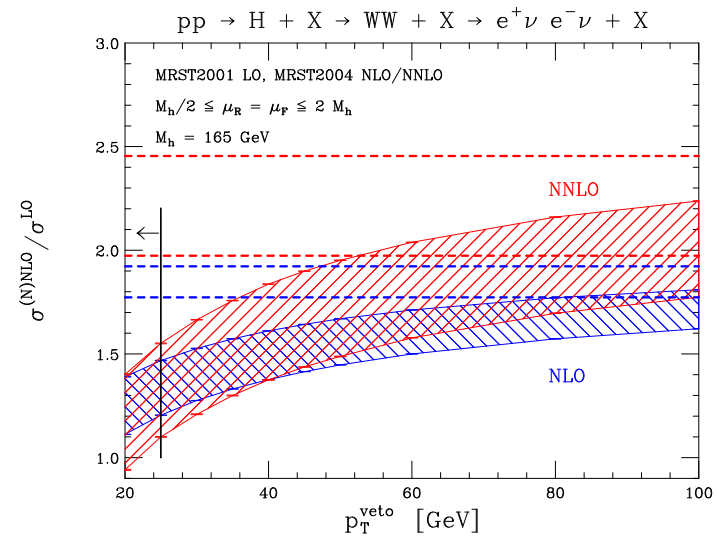
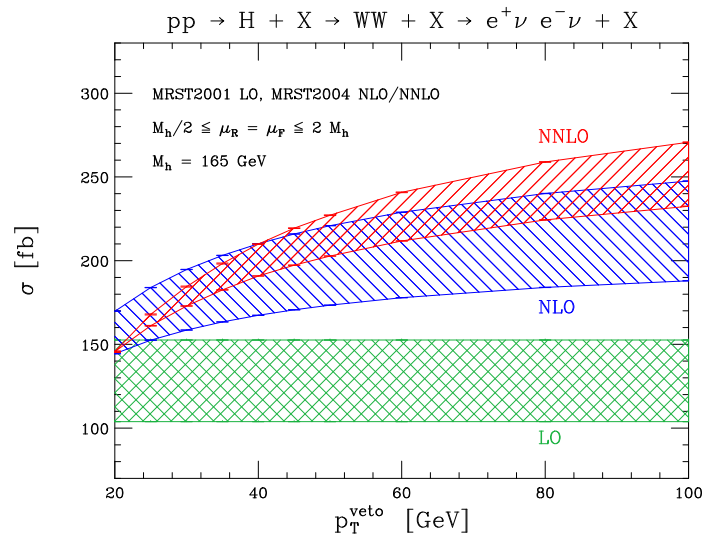


[Anastasiou, Melnikov, Petriello (05)]

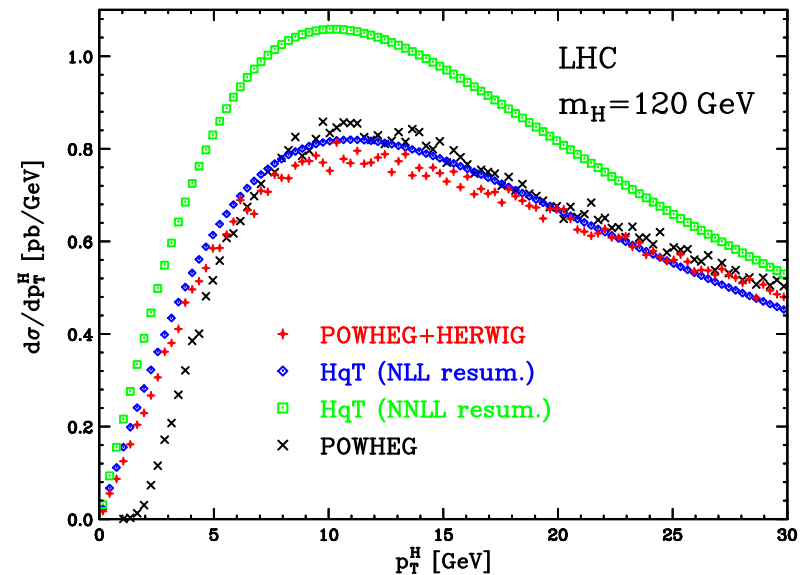
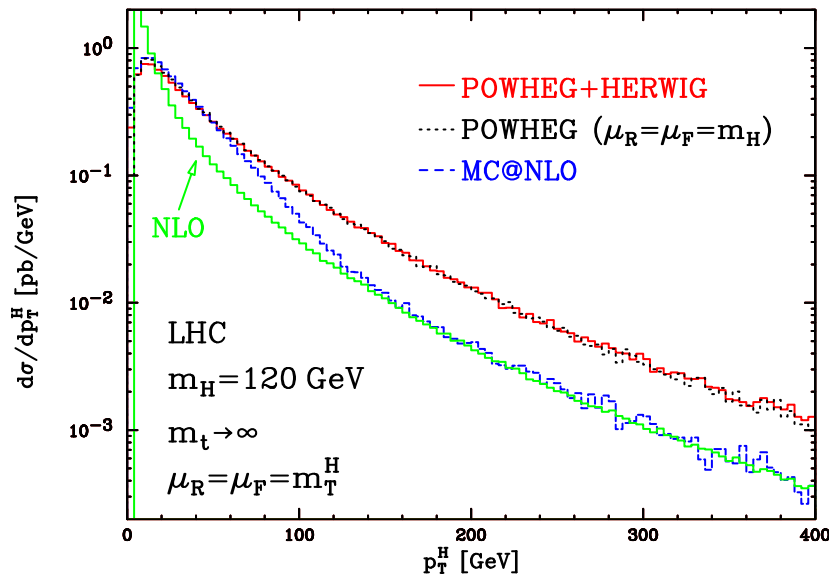
jet veto (to enhance  $H \rightarrow WW$  signal with respect to  $t\bar{t}$  background) seems to improve perturbative stability of  $y$ -distribution → jet veto is removing non-NNLO contributions.

# Full fledged $(gg \rightarrow)H \rightarrow W^+W^- \rightarrow l^+\nu l^-\bar{\nu}$

The magnitude of higher order corrections varies significantly with the signal selection cuts.



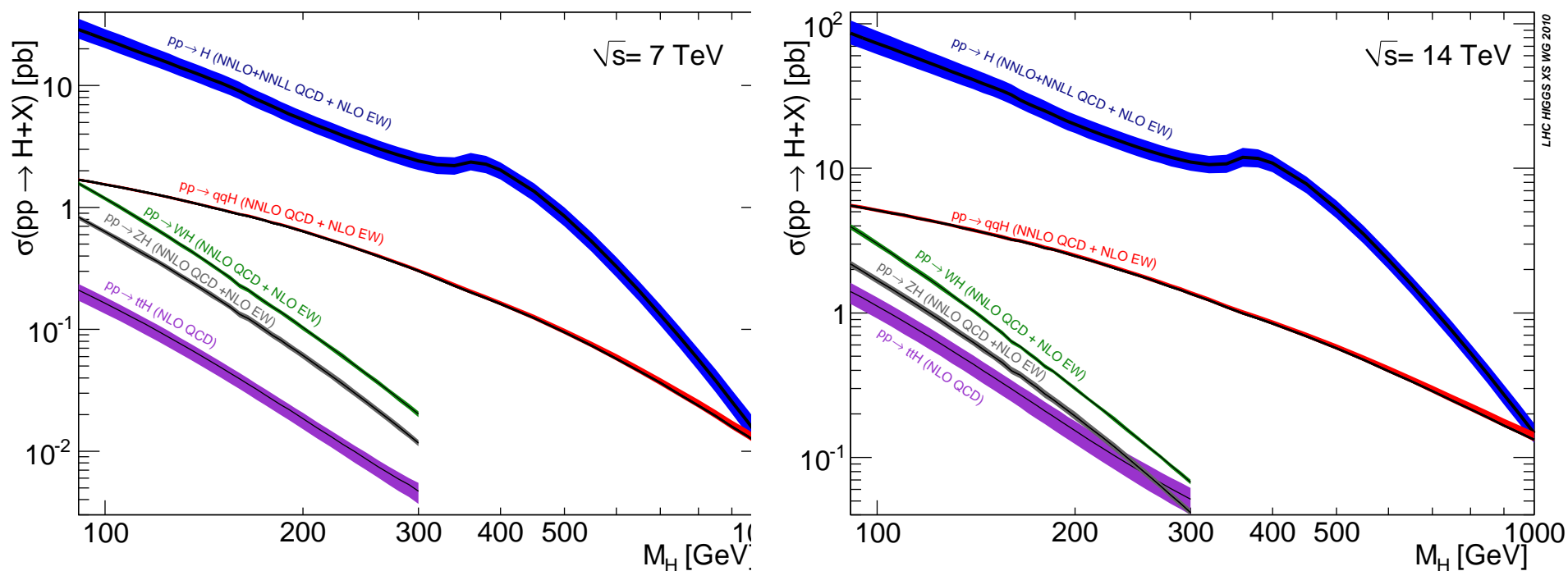
# $gg \rightarrow H$ implemented in MC@NLO and POWHEG



[Nason, Oleari, Alioli, Re]

- general good agreement with PYTHIA;
- comparison MC@NLO vs POWHEG understood;
- comparison with resummed NLL and NNLL results under control.

## Ex. 4: Inclusive SM Higgs Production: theoretical predictions and their uncertainty



(LHC Higgs Cross Sections Working Group, arXiv:1101.0593 → CERN Yellow Book)

- ↪ all orders of calculated higher orders corrections included (tested with all existing calculations);
- ↪ common recipe for renormalization+factorization scale dependence;
- ↪ PDF and  $\alpha_s$  errors following PDF4LHC prescription ( → see **de Florian**'s talk);
- ↪ all other parametric errors included;
- ↪ theory errors combined according to common recipe.



For  $\sqrt{s} = 7$  TeV (from S. Dittmaier's talk, BNL, May 2011)

	$M_H$	Uncertainties		NLO/NNLO/NNLO+	
		scale	PDF4LHC	QCD	EW
ggF	< 500 GeV	6-10%	8-10%	> 100%	5%
VBF	< 500 GeV	1%	2-7%	5%	5%
$WH$	< 300 GeV	1%	3-4%	30%	5-10%
$ZH$	< 300 GeV	1-2%	3-4%	40%	5%
$t\bar{t}H$	< 300 GeV	10%	9%	5%	?

For  $\sqrt{s} = 14$  TeV

	$M_H$	Uncertainties		NLO/NNLO/NNLO+	
		scale	PDF4LHC	QCD	EW
ggF	< 500 GeV	6-14%	7%	> 100%	5%
VBF	< 500 GeV	1%	3-4%	5%	5%
$WH$	< 300 GeV	1%	3-4%	30%	5-10%
$ZH$	< 300 GeV	2-4%	3-4%	45%	5%
$t\bar{t}H$	< 300 GeV	10%	9%	15-20%	?