

# Strings and Unification

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# Questions

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- Can we incorporate particle physics models within the framework of string theory?

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- Can we incorporate particle physics models within the framework of string theory?

## Recent progress:

- explicit model building towards the MSSM
  - Heterotic brane world
  - local grand unification
- moduli stabilization and Susy breakdown
  - gaugino condensation and uplifting
  - mirage mediation

# The road to the Standard Model

What do we want?

- gauge group  $SU(3) \times SU(2) \times U(1)$
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- scalar Higgs doublet

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But there might be more:

- supersymmetry (SM extended to MSSM)
- neutrino masses and mixings

as a hint for a large mass scale around  $10^{16}$  GeV

# Indirect evidence

Experimental findings suggest the existence of two new scales of physics beyond the standard model

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- **Neutrino-oscillations** and “See-Saw Mechanism”

$$m_\nu \sim M_W^2 / M_{\text{GUT}}$$

$$m_\nu \sim 10^{-3} \text{eV for } M_W \sim 100 \text{GeV,}$$

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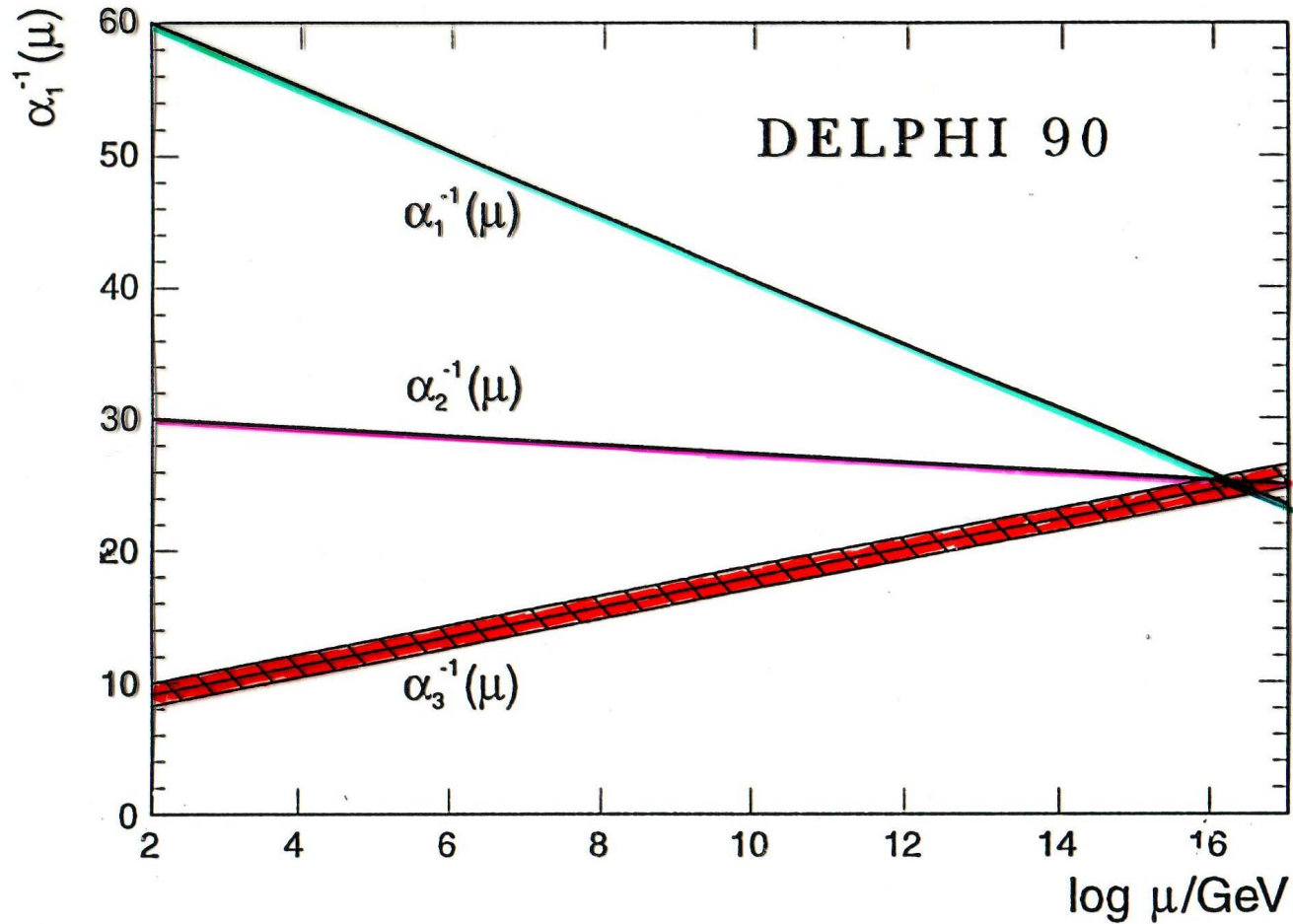
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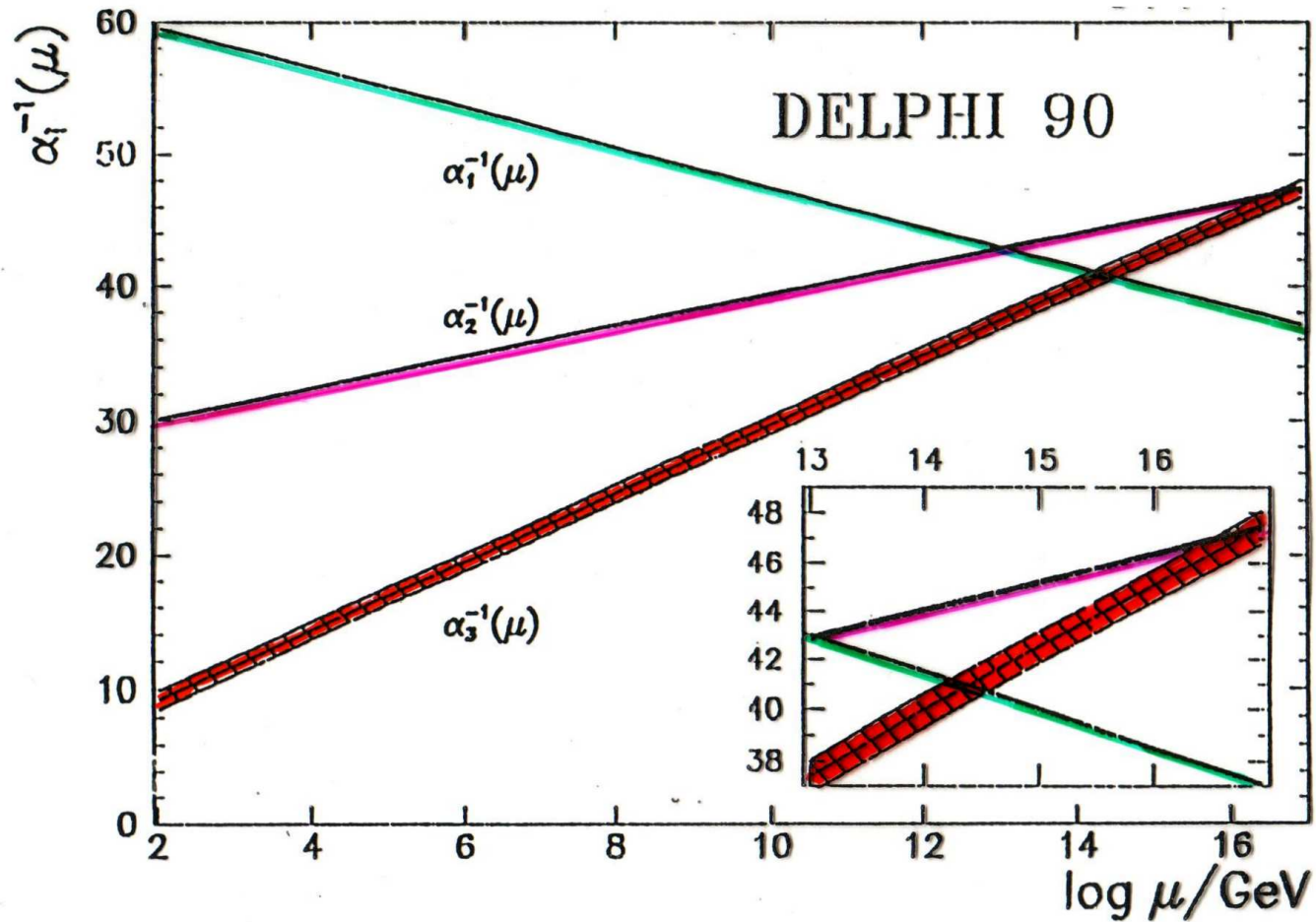
- **Evolution of couplings constants** of the standard model towards higher energies.



# MSSM (supersymmetric)



# Standard Model



# Grand Unification

This leads to SUSY-GUTs with nice things like

- unified multiplets (e.g. **spinors of  $SO(10)$** )
- gauge coupling unification
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But there remain a few difficulties:

- breakdown of GUT group (large representations)
- doublet-triplet splitting problem (incomplete multiplets)
- proton stability (need for R-parity)

# String Theory

What do we get from string theory?

- supersymmetry
- extra spatial dimensions
- large unified gauge groups
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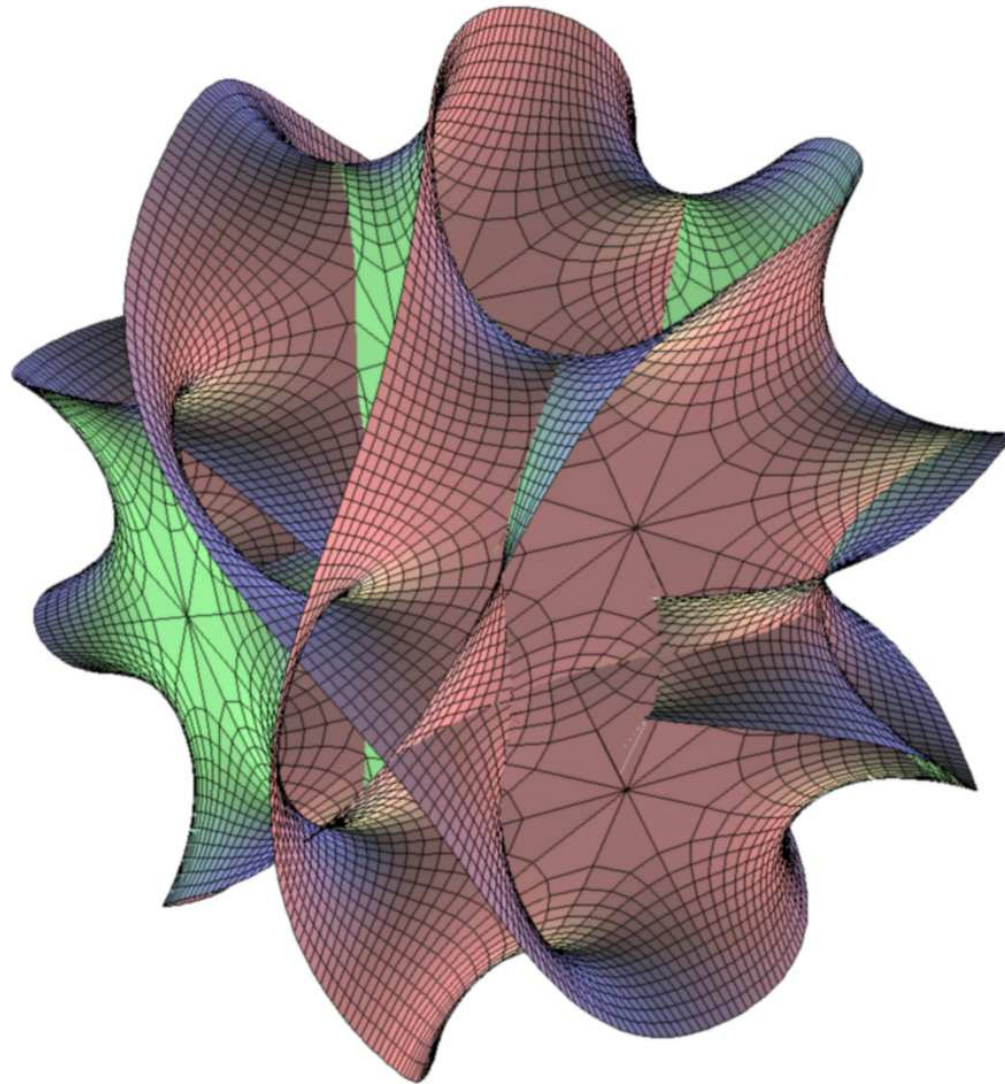
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These are the building blocks for a **unified theory** of all the fundamental interactions.

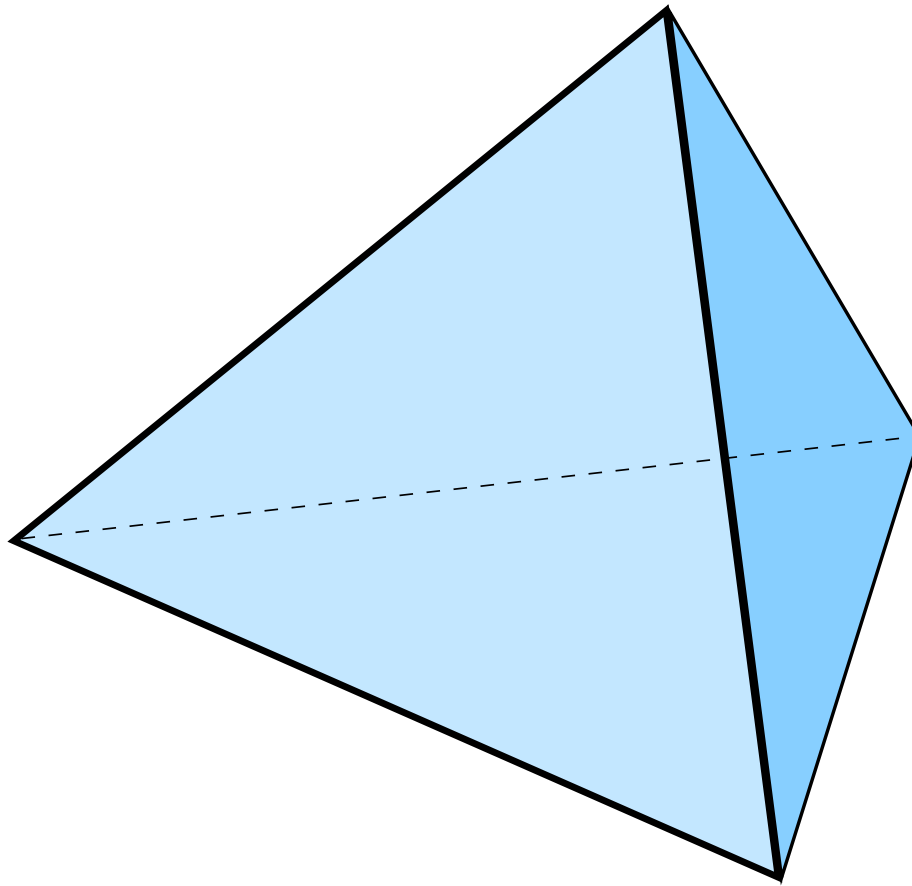
But do they fit together, and if yes how?

**We need to understand the mechanism of compactification of the extra spatial dimensions**

# Calabi Yau Manifold



# Orbifold





# Localization

Quarks, Leptons and Higgs fields can be localized:

- in the Bulk ( $d = 10$  **untwisted** sector)
- on 3-Branes ( $d = 4$  twisted sector **fixed points**)
- on 5-Branes ( $d = 6$  twisted sector **fixed tori**)

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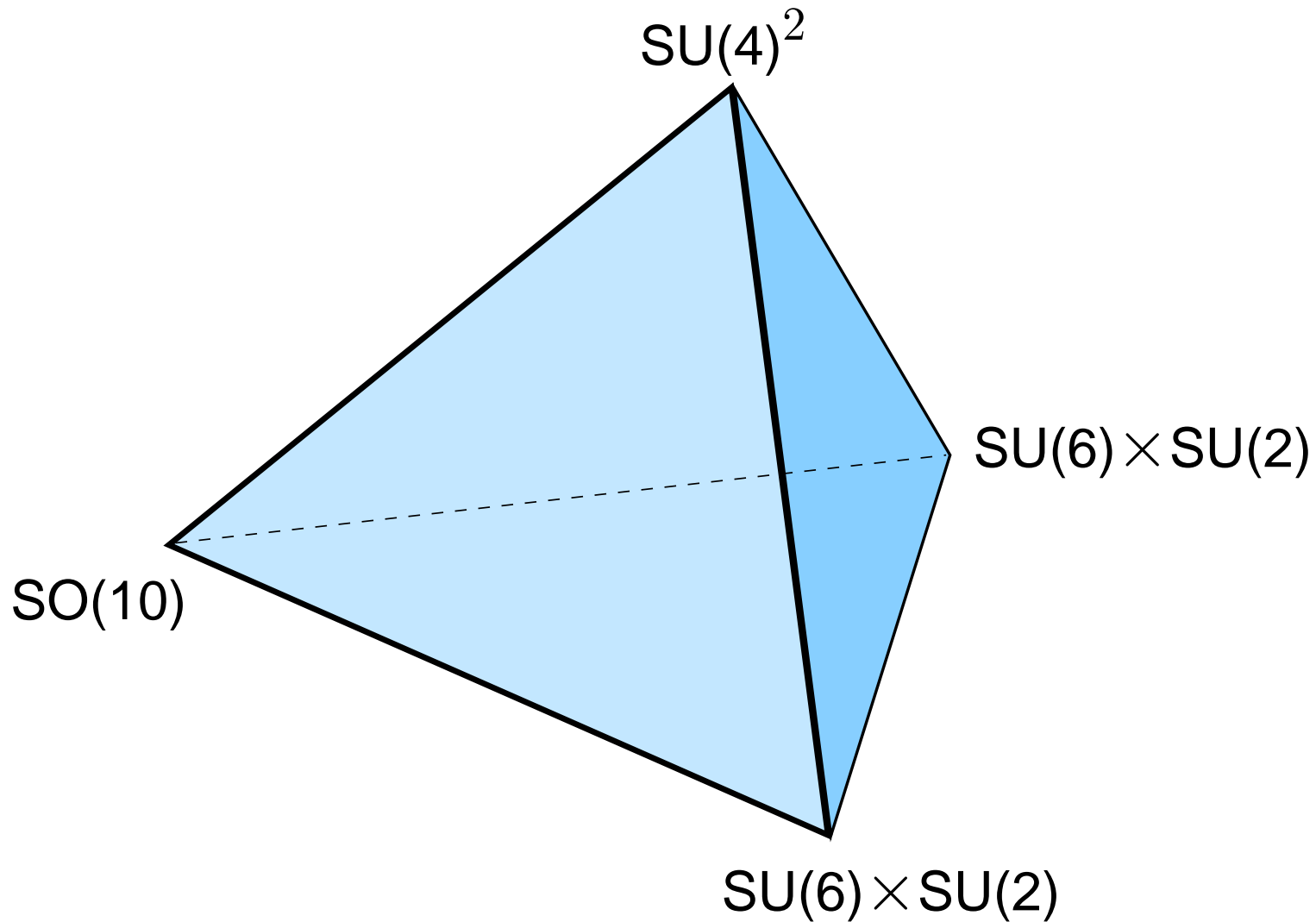
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but there is also a “localization” of gauge fields

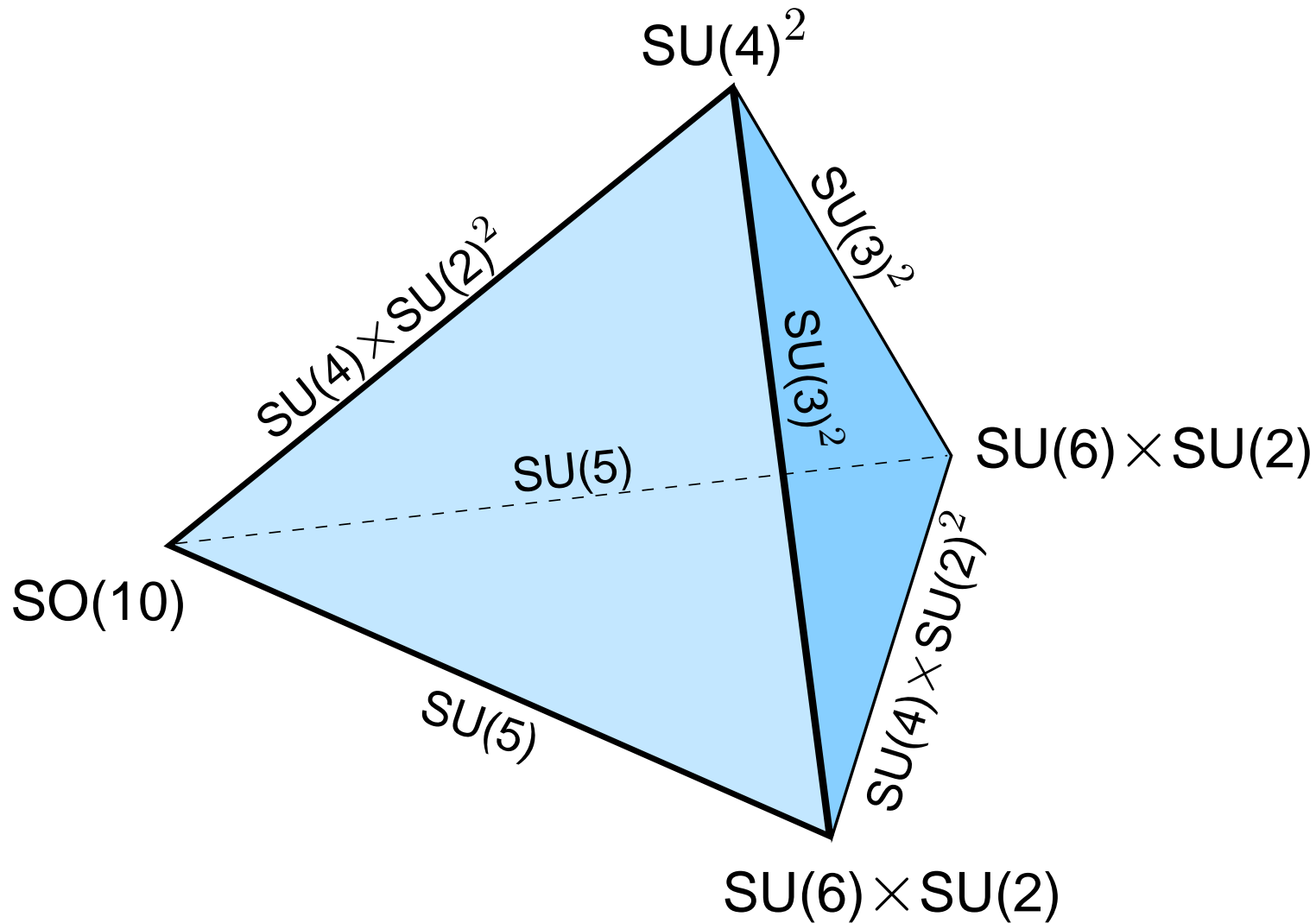
- $E_8 \times E_8$  in the bulk
- smaller gauge groups on various branes

Observed 4-dimensional gauge group is common subgroup of the various localized gauge groups!

# Localized gauge symmetries



# Standard Model Gauge Group



# Local Grand Unification

In fact string theory gives us a variant of GUTs

- complete multiplets for fermion families
- split multiplets for gauge- and Higgs-bosons
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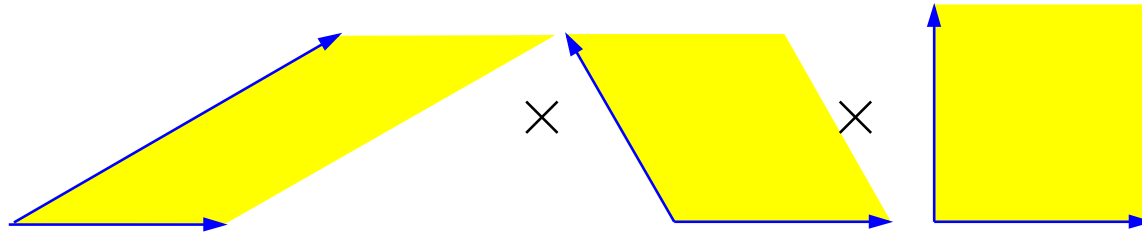
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Key properties of the theory depend on the **geography** of the fields in extra dimensions.

This geometrical set-up called **local GUTs**, can be realized in the framework of the “heterotic braneworld”.

(Förste, HPN, Vaudrevange, Wingerter, 2004; Buchmüller, Hamaguchi, Lebedev, Ratz, 2004)

# The “fertile patch”: $Z_6$ II orbifold



(Kobayashi, Raby, Zhang, 2004; Buchmüller, Hamaguchi, Lebedev, Ratz, 2004)

- provides fixed points and fixed tori
- allows  $SO(10)$  gauge group
- allows for **localized 16-plets** for 2 families
- $SO(10)$  broken via Wilson lines
- nontrivial hidden sector gauge group

# Selection Strategy

criterion	$V^{\text{SO}(10),1}$	$V^{\text{SO}(10),2}$
② models with 2 Wilson lines	22,000	7,800
③ SM gauge group $\subset \text{SO}(10)$	3563	1163
④ 3 net families	1170	492
⑤ gauge coupling unification	528	234
⑥ no chiral exotics	128	90

(Lebedev, HPN, Raby, Ramos-Sanchez, Ratz, Vaudrevange, Wingerter, 2006)



# The road to the MSSM

This scenario leads to

- 200 models with the **exact spectrum of the MSSM** (absence of chiral exotics)

- **local grand unification** (by construction)

- gauge- and (partial) Yukawa unification

(Raby, Wingerter, 2007)

- examples of **neutrino see-saw mechanism**

(Buchmüller, Hamguchi, Lebedev, Ramos-Sanchez, Ratz, 2007)

- models with **R-parity** + solution to the  $\mu$ -problem

(Lebedev, HPN, Raby, Ramos-Sanchez, Ratz, Vaudrevange, Wingerter, 2007)

- gaugino condensation and **mirage mediation**

(Löwen, HPN, 2008)

# A Benchmark Model

At the orbifold point the gauge group is

$$SU(3) \times SU(2) \times U(1)^9 \times SU(4) \times SU(2)$$

- one  $U(1)$  is anomalous
- there are singlets and vectorlike exotics
- decoupling of exotics and breakdown of gauge group has been verified
- remaining gauge group

$$SU(3) \times SU(2) \times U(1)_Y \times SU(4)_{\text{hidden}}$$

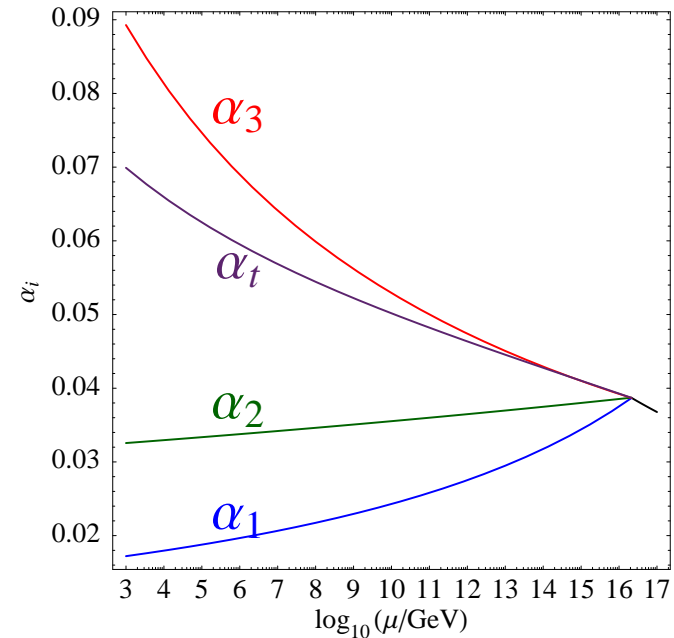
- for discussion of neutrinos and R-parity we keep also the  $U(1)_{B-L}$  charges

# Spectrum

#	irrep	label	#	irrep	label
3	$(\mathbf{3}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(1/6, 1/3)}$	$q_i$	3	$(\bar{\mathbf{3}}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-2/3, -1/3)}$	$\bar{u}_i$
3	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1, 1)}$	$\bar{e}_i$	8	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(0, *)}$	$m_i$
3 + 1	$(\bar{\mathbf{3}}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1/3, -1/3)}$	$\bar{d}_i$	1	$(\mathbf{3}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-1/3, 1/3)}$	$d_i$
3 + 1	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(-1/2, -1)}$	$l_i$	1	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(1/2, 1)}$	$\bar{l}_i$
1	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(-1/2, 0)}$	$h_d$	1	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(1/2, 0)}$	$h_u$
6	$(\bar{\mathbf{3}}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1/3, 2/3)}$	$\bar{\delta}_i$	6	$(\mathbf{3}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-1/3, -2/3)}$	$\delta_i$
14	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1/2, *)}$	$s_i^+$	14	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-1/2, *)}$	$s_i^-$
16	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(0, 1)}$	$\bar{n}_i$	13	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(0, -1)}$	$n_i$
5	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{2})_{(0, 1)}$	$\bar{\eta}_i$	5	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{2})_{(0, -1)}$	$\eta_i$
10	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{2})_{(0, 0)}$	$h_i$	2	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{2})_{(0, 0)}$	$y_i$
6	$(\mathbf{1}, \mathbf{1}; \mathbf{4}, \mathbf{1})_{(0, *)}$	$f_i$	6	$(\mathbf{1}, \mathbf{1}; \bar{\mathbf{4}}, \mathbf{1})_{(0, *)}$	$\bar{f}_i$
2	$(\mathbf{1}, \mathbf{1}; \mathbf{4}, \mathbf{1})_{(-1/2, -1)}$	$f_i^-$	2	$(\mathbf{1}, \mathbf{1}; \bar{\mathbf{4}}, \mathbf{1})_{(1/2, 1)}$	$\bar{f}_i^+$
4	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(0, \pm 2)}$	$\chi_i$	32	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(0, 0)}$	$s_i^0$
2	$(\bar{\mathbf{3}}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-1/6, 2/3)}$	$\bar{v}_i$	2	$(\mathbf{3}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1/6, -2/3)}$	$v_i$

# Unification

- Higgs doublets are in untwisted (U3) sector
- trilinear coupling to the top-quark allowed
- threshold corrections (“on third torus”) allow unification at correct scale around  $10^{16}$  GeV



(Hosteins, Kappl, Ratz, Schmidt-Hoberg, 2009)

# See-saw neutrino masses

The see-saw mechanism requires

- right handed neutrinos ( $Y = 0$  and  $B - L = \pm 1$ ),
- heavy Majorana neutrino masses  $M_{\text{Majorana}}$ ,
- Dirac neutrino masses  $M_{\text{Dirac}}$ .

The benchmark model has 49 right handed neutrinos:

- the left handed neutrino mass is  $m_\nu \sim M_{\text{Dirac}}^2 / M_{\text{eff}}$
- with  $M_{\text{eff}} < M_{\text{Majorana}}$  and depends on the number of right handed neutrinos.

(Buchmüller, Hamguchi, Lebedev, Ramos-Sanchez, Ratz, 2007;  
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# R-parity

- R-parity allows the **distinction** between Higgs bosons and sleptons
- $SO(10)$  **contains R-parity** as a discrete subgroup of  $U(1)_{B-L}$ .
- in conventional “**field theory GUTs**” one needs large representations to break  $U(1)_{B-L}$  ( $\geq 126$  dimensional)
- in **heterotic string** models one has more candidates for R-parity (and generalizations thereof)
- one just needs **singlets with an even  $B - L$  charge** that **break  $U(1)_{B-L}$  down to R-parity**

(Lebedev, HPN, Raby, Ramos-Sanchez, Ratz, Vaudrevange, Wingerter, 2007)

# Discrete Symmetries

There are numerous discrete symmetries:

- from geometry
- and stringy selection rules,
- both of abelian and nonabelian nature

(Kobayashi, HPN, Plöger, Raby, Ratz, 2006)

The importance of these discrete symmetries cannot be underestimated. After all, besides the gauge symmetries this is what we get in string theory.

At low energies the discrete symmetries might appear as accidental continuous global  $U(1)$  symmetries.



# Accidental Symmetries

Applications of discrete and accidental global symmetries:

- (nonabelian) family symmetries (and FCNC)

(Ko, Kobayashi, Park, Raby, 2007)

- Yukawa textures (via Frogatt-Nielsen mechanism)

- a solution to the  $\mu$ -problem

(Lebedev, HPN, Raby, Ramos-Sanchez, Ratz, Vaudrevange, Wingerter, 2007)

- creation of hierarchies

(Kappl, HPN, Ramos-Sanchez, Ratz, Schmidt-Hoberg, Vaudrevange, 2008)

- proton stability via “Proton Hexality”

(Dreiner, Luhn, Thormeier, 2005; Förste, HPN, Ramos-Sanchez, Vaudrevange, 2009)

- approximate global  $U(1)$  for a QCD action

(Choi, Kim, Kim, 2006; Choi, HPN, Ramos-Sanchez, Vaudrevange, 2008)

# The $\mu$ problem

In general we have to worry about

- doublet-triplet splitting
- mass term for additional doublets
- the appearance of “naturally” light doublets

In the benchmark model we have

- only 2 doublets
- which are neutral under all selection rules
- if  $M(s_i)$  allowed in superpotential
- then  $M(s_i)H_uH_d$  is allowed as well

# The $\mu$ problem II

We have verified that (up to order 6 in the singlets)

- $F_i = 0$  implies automatically
- $M(s_i) = 0$  for all allowed terms  $M(s_i)$  in the superpotential  $W$

Therefore

- $W = 0$  in the supersymmetric (Minkowski) vacuum
- as well as  $\mu = \partial^2 W / \partial H_u \partial H_d = 0$ , while all the vectorlike exotics decouple
- with broken supersymmetry  $\mu \sim m_{3/2} \sim \langle W \rangle$

This solves the  $\mu$ -problem

(Casas, Munoz, 1993)

# The creation of the hierarchy

Is there an explanation for a vanishing  $\mu$ ?

- string miracle?
- underlying symmetry?

Consider a superpotential

$$W = \sum c_{n_1 \dots n_M} \phi_1^{n_1} \dots \phi_M^{n_M} .$$

with an exact R-symmetry

$$W \rightarrow e^{2i\alpha} W , \quad \phi_j \rightarrow \phi'_j = e^{i r_j \alpha} \phi_j$$

where each monomial in  $W$  has total R-charge 2.

# ...hierarchy continued...

Consider a field configuration  $\langle \phi_i \rangle$  with

$$F_i = \frac{\partial W}{\partial \phi_i} = 0 \quad \text{at } \phi_j = \langle \phi_j \rangle \quad \forall i, j .$$

Under an infinitesimal  $U(1)_R$  transformation, the superpotential transforms nontrivially

$$W(\phi_j) \rightarrow W(\phi'_j) = W(\phi_j) + \sum_i \frac{\partial W}{\partial \phi_i} \Delta \phi_i .$$

This proves that, if the  $F = 0$  equations are satisfied,  $W$  vanishes at the minimum (as a consequence of a continuous R-symmetry)

# Continuous R-symmetry

Thus for a continuous R-symmetry we would have

- a supersymmetric ground state with  $W = 0$  and  $U(1)_R$  spontaneously broken
- a problematic R-Goldstone-Boson

However, the above R-symmetry appears as an accidental continuous symmetry resulting from an exact discrete symmetry of (high) order  $N$

- Goldstone-Boson massive and harmless
- a nontrivial VEV of  $W$  of higher order in  $\phi$

(Kappl, HPN, Ramos-Sanchez, Ratz, Schmidt-Hoberg, Vaudrevange, 2008)

# Hierarchy

Such accidental symmetries lead to

- creation of a **small constant in the superpotential**
- explanation of a **small  $\mu$  term**

(Kappl, HPN, Ramos-Sanchez, Ratz, Schmidt-Hoberg, Vaudrevange, 2008)

Even with a moderate hierarchy like  $\phi/M_P \sim 10^{-2}$  one can generate small values for  $\mu$  and  $\langle W \rangle$  and thus a hierarchically small **TeV-scale for the gravitino mass**

$$m_{3/2} \sim W_{\text{eff}} = c + A e^{-a S}$$

in the framework of a **modulus or mirage mediation scheme** of supersymmetry breakdown.

(Löwen, HPN, 2008)

# Accions

Absence of continuous global  $U(1)$  symmetries in string theory leads to a question towards the

- axion as a solution to the strong CP-problem

A gauge anomalous  $U(1)$  symmetry might help, but there we expect

- a too large axion decay constant of order of string scale

Again additional accidental global  $U(1)$  symmetries arising as a consequence of discrete symmetries might help,

(Choi, Kim, Kim, 2007; Choi, HPN, Ramos-Sanchez, Vaudrevange, 2009)

but we need to control the axion scale  $F_a$ .



# Multi-Axion Systems

Consider a system with **two  $U(1)$  symmetries**:  $U(1)_P \times U(1)_Q$  and suppose that they are broken spontaneously.

$$F_{a_1} = -v_1 \frac{q_P^1 q_Q^2 - q_Q^1 q_P^2}{q_f^2}, \quad F_{a_2} = v_2 \frac{q_P^1 q_Q^2 - q_Q^1 q_P^2}{q_f^1}.$$

The relevant **accion decay constant** will then be

$$F_a = \left( \left( \frac{1}{F_{a_1}} \right)^2 + \left( \frac{1}{F_{a_2}} \right)^2 \right)^{-1/2} = \frac{v_1 v_2 (q_P^1 q_Q^2 - q_Q^1 q_P^2)}{\sqrt{(q_f^1 v_1)^2 + (q_f^2 v_2)^2}}.$$

**and it is dominated by the smallest VEV!**

# The Accion Program

- find a model with an **accidental** (colour)-anomalous  $U(1)^*$
- identify a vacuum configuration where the VEVs driven by the Fayet-Iliopoulos term **do not break**  $U(1)^*$
- search for a vacuum configuration where  $U(1)^*$  is broken by a **VEV in the axion window** (some other gauge  $U(1)$ 's might be broken here as well)
- check that higher order non-renormalizable terms that break  $U(1)^*$  explicitly are **sufficiently suppressed to avoid a too “large” axion mass.**

(Choi, HPN, Ramos-Sanchez, Vaudrevange, 2009)

can be accomodated in the Heterotic Brane World.

# Conclusion

String theory provides us with **new ideas for particle physics** model building, leading to concepts such as

- **MSSM via Local Grand Unification**
- **Accidental symmetries (of discrete origin)**

**Geography of extra dimensions** plays a crucial role:

- **localization** of fields on branes,
- **sequestered sectors and mirage mediation**

**We seem to live at a special place in the extra dimensions!**

The LHC might clarify the case for (local) grand unification.